## Supplementary Material

## Racial/Ethnic Disparities in the Alzheimer's Disease Link with Cardio and Cerebrovascular Diseases, based on Hawaii Medicare Data

## Estimations and testings of multistate models

In our approach, we estimated transition hazard functions using the Nelson Aalen hazard rate estimator and next used the Aalen-Johansen product limit integral estimator to quantify marginal estimates of state occupation probabilities, which are nonparametric techniques that provide a great flexibility of handling multistate system without strict model assumptions [1-3]. Below we provide a general explanation of the estimation procedure.

Consider a general time continuous multistate model with a finite state $k=\{0, . ., K\}$, that allows a set of transitions among states. Note that, in the current problem, the initial state is indicated by 0 and $K$ is fixed to be $t$ wo. Suppose that a set of $n$ individuals move independently in the multistate system starting from state 0 . In the current illness and death model, at time 0 , there is no subjects present in state 1 or 2 . For the $i$ th individual, $i=1, \ldots, n$, suppose $S_{i}(t)$ is the state occupies by the individual at time $t$ and let $T_{i}^{*}$ be the time required for the individual to reach the absorbing state (i.e., state $K$ ) and $C_{i}$ be the right censoring time. Note $T_{i}=\min \left\{T_{i}^{*}, C_{i}\right\}$ is the observed time for the $i$ th subject. Say $\delta_{i}=I\left(C_{i} \geq T_{i}^{*}\right)$ is the right-censoring indicator with respect to reaching the absorbing state for the individual. Define $X_{i}=\left(X_{i 1}, . ., X_{i p}\right)^{T}$ a $p$ dimensional covariate vector contains baseline information of the individual. Thus, the observed data consist of independently and identically distributed copies of $\left\{S_{i}(t), 0 \leq t \leq T_{i}, \delta_{i}, X_{i}\right\}$, $1 \leq i \leq n$, for $n$ subjects.

The state to state transition counting process $N_{k k^{\prime}}(t)$ correspond to $k$ to $k^{\prime}$ at time point $t$ is given by

$$
N_{k k^{\prime}}(t)=\sum_{i=1}^{n} I\left(C_{i} \geq t, S_{i}(t-)=k, S_{i}(t)=k^{\prime}\right)
$$

where $S_{i}(t-)=\lim _{v \rightarrow t-} S_{i}(v)$ is the state that $i$ th subject presented just prior to time $t$. The at-risk process correspond to $k$ th state $Y_{k}(t)$ at $t$ is given by,

$$
Y_{k}(t)=\sum_{i=1}^{n} I\left(C_{i} \geq t, S_{i}(t-)=k\right)
$$

Next, using the two temporal $N_{k k^{\prime}}(t)$ and $Y_{k}(t)$, the Nelson-Aalen estimate of cumulative (integrated) state to state transition hazard $\hat{A}_{j j^{\prime}}(t)$ is estimated as follows:

$$
\hat{A}_{k k^{\prime}}(t)= \begin{cases}\int_{0}^{t} W(v) \hat{Y}_{k}(v)^{-1} d \hat{N}_{k k^{\prime}}(v), & \text { if } k \neq k^{\prime} \\ -\sum_{k \neq k^{\prime}} \hat{A}_{k k^{\prime}}(t), & \text { otherwise }\end{cases}
$$

where $W(v)=I\left(\hat{Y}_{j}(v)>0\right)$ and $I($.$) is an indicator function. The counting process$ given by $d \hat{N}_{k k^{\prime}}(t)$ is obtained by the corresponding increments of state-to-state transitions at $[t-, t)$ window. The above transition hazard estimation allows one to obtain an estimate of cumulative transition matrix of the multistate system, followed by the product limit integral

$$
\hat{P}(s, t)=\prod_{(s, t]}\left(I_{K}+d \hat{A}\right)
$$

with $I_{K}, K \times K$ dimensional identity matrix. The marginal estimator of $k$ th state occupation probability $p_{k}(t)=\operatorname{Prob} .[S(t)=k]$ for $k=1, . ., K$ is given by,

$$
\hat{p}_{k}(t)=\sum_{j=0}^{K} \frac{\hat{Y}_{j}(0+)}{n} \hat{p}_{j k}(0, t)
$$

where $\hat{p}_{j k}(0, t)$ is the $(j, k)$ th element of the matrix $\hat{P}(0, t)$. Note: the validity of such estimation formulas for non-Markov models have been established in the literature.

In order to test effects of covariates on state temporal functions of multistate models, method given by the pseudo-values regression, by Anderson and Klein [4] was applied. This method utilizes a pseudo-values based regression concept that initiated with a marginal estimator of the targeted quantity, which could be both parametric or nonparametric, followed by a jackknife estimation process together with flexible generalized estimating equations (GEE) inferencing. A key advantage of this approach is the straightforward interpretation of covariate effects on the measure of interest. The jackknife estimator of the measure of interest at time $t, Q(i)$ is obtained by,

$$
\hat{Q}_{i}^{p s}(t)=n \hat{Q}(t)-(n-1) \hat{Q}^{-i}(t)
$$

where $\hat{Q}^{-i}(t)$ is the marginal estimator that obtained from a sample of size $n-1$ by excluding the $i$ th individual data and $\hat{Q}(t)$ is the corresponding estimate calculated from the whole dataset. For example $\hat{Q}(t)$ will be the marginal state occupation probability estimator at a given time $t$ by the Aalen and Johansen, when the measure of interest is state occupation probability [4]. The estimated observed pseudo values at a time grid value are next fitted in a regression model by incorporating the covariates of interest together with a suitable link function and estimated the model via the GEE approach. In this work, we used the GEE model with a complementary $\log -\log$ link function to estimate the covariate effect.

Supplementary Table 1: The set of ICD 9 and ICD 10 codes used to specify disease conditions.

| Atrial fibrillation (AF) | ICD9: 427.3; ICD10: I48.0 I48.1, I48.2, I48.3. I48.4 |
| :--- | :--- |
| Acute myocardial infarction (AMI) | ICD9: 410.X; ICD10: I21.X |
| Heat Failure (HF) | ICD9: 428.X; ICD10: I50.X |
| Ischemic Heart Disease (IHD) | ICD9: 414.X; ICD10: I25.X |
| Stroke | ICD9: 433.X, 434.X; ICD10: I63.5, I63.9 |
| Alzheimer's Disease (AD) | ICD9: 331.0; ICD10: G30.0, G30.1, G30.9, G30.8 |

Supplementary Table 2: A summary of subject characteristics among individuals with the initial event: Atrial Fibrillation (AF), corresponds to the multistate model given in Fig. 1.

|  | Diseased set | Control |
| :--- | :--- | :--- |
| Total number of individuals | 12,991 | 12,991 |
| Age (average, SD) | $76.76(7.85)$ | $76.76(7.85)$ |
| Gender: Male | $7,452(57.36 \%)$ | $7,301(56.20 \%)$ |
| Race/Ethnicity | Whites | $4,512(34.73 \%)$ |
|  | Asian | $3,788(36.86 \%)$ |
|  | Other | $2,847(21.54 \%)$ |
| $2,950(22.71 \%)$ |  |  |
| Dual Eligibility | $2,444(18.81 \%)$ | $2,871(22.10 \%)$ |
| Chronic Kidney Disease | $2,145(16.51 \%)$ | $2,057(15.33 \%)$ |
| Cataract | $2,459(18.93 \%)$ | $2,032(15.64 \%)$ |
| Chronic Obstructive Pulmonary Disease | $5,734(44.14 \%)$ | $5,246(40.38 \%)$ |
| Diabetes | $4,003(15.42 \%)$ | $2,172(16.72 \%)$ |
| Glaucoma | $2,332(17.99 \%)$ | $3,985(30.68 \%)$ |
| Hip/Pelvic Fracture | $171(1.32 \%)$ | $2,094(16.12 \%)$ |
| Depression | $1,240(9.55 \%)$ | $989(7.38 \%)$ |
| Osteoporosis | $1,842(14.18 \%)$ | $1,565(12.05 \%)$ |
| Rheumatoid Arthritis / Osteoarthritis | $3,480(26.79 \%)$ | $3,793(29.20 \%)$ |
| Anemia | $4,716(36.30 \%)$ | $4,690(36.10 \%)$ |
| Asthma | $1,399(10.77 \%)$ | $1,636(12.61 \%)$ |
| Hyperlipidemia | $7,865(60.54 \%)$ | $7,557(58.17 \%)$ |
| Hypertension | $8,354(64.31 \%)$ | $7,810(60.12 \%)$ |
| Acquired Hypothyroidism | $1,190(9.16 \%)$ | $912(7.02 \%)$ |
| Cancer Breast (among females) | $451(8.14 \%)$ | $594(10.44 \%)$ |
| Cancer Colorectal | $282(2.17 \%)$ | $460(3.54 \%)$ |
| Cancer Lung | $141(1.09 \%)$ | $299(2.30 \%)$ |
| Cancer Endometrial | $63(0.48 \%)$ | $118(0.91 \%)$ |

Data are summarized using frequencies and percentages, unless specified otherwise.

Supplementary Table 3: A summary of subject characteristics among individuals with the initial event: Acute Myocardial Infarction (AMI), corresponds to the multistate model given in Fig. 1.

|  | Diseased set | Control |
| :--- | :--- | :--- |
| Total number of individuals | 7,856 | 7,856 |
| Age (average, SD) | $77.15(7.92)$ | $77.15(7.92)$ |
| Gender: Male | $4,603(58.59 \%)$ | $4,659(59.30 \%)$ |
| Race/Ethnicity | Whites | $2,171(27.63 \%)$ |
|  | Asian | $2,241(28.53 \%)$ |
|  | NHPI | $1,864(27.91 \%)$ |
|  | $2,113(26.90 \%)$ |  |
| Dual Eligibility | $1,628(20.72 \%)$ | $1,842(23.45 \%)$ |
| Chronic Kidney Disease | $1,474(18.76 \%)$ | $1,404(21.13 \%)$ |
| Cataract | $2,170(27.62 \%)$ | $2,036(25.92 \%)$ |
| Chronic Obstructive Pulmonary Disease | $3,645(46.40 \%)$ | $3,775(48.05 \%)$ |
| Diabetes | $3,247(17.04 \%)$ | $1,213(15.44 \%)$ |
| Glaucoma | $1,518(19.32 \%)$ | $3,152(40.12 \%)$ |
| Hip/Pelvic Fracture | $116(1.48 \%)$ | $71(0.90 \%)$ |
| Depression | $753(9.59 \%)$ | $678(8.63 \%)$ |
| Osteoporosis | $1,126(14.33 \%)$ | $1,186(15.10 \%)$ |
| Rheumatoid Arthritis / Osteoarthritis | $2,172(27.65 \%)$ | $2,193(27.91 \%)$ |
| Anemia | $3,406(43.36 \%)$ | $3,191(40.62 \%)$ |
| Asthma | $947(12.05 \%)$ | $845(10.75 \%)$ |
| Hyperlipidemia | $5,315(67.66 \%)$ | $5,199(66.18 \%)$ |
| Hypertension | $5,571(70.91 \%)$ | $5,436(69.20 \%)$ |
| Acquired Hypothyroidism | $711(9.05 \%)$ | $672(8.55 \%)$ |
| Cancer Breast (among females) | $264(8.12 \%)$ | $229(7.15 \%)$ |
| Cancer Colorectal | $180(2.29 \%)$ | $212(2.70 \%)$ |
| Cancer Lung | $78(0.99 \%)$ | $125(1.59 \%)$ |
| Cancer Endometrial | $34(0.43 \%)$ | $26(0.33 \%)$ |

Data are summarized using frequencies and percentages, unless specified otherwise.

Supplementary Table 4: A summary of subject characteristics among individuals with the initial event: Heart Failure (HF), corresponds to the multistate model given in Fig. 1.

|  | Diseased set | Control |
| :--- | :--- | :--- |
| Total number of individuals | 10,748 | 10,748 |
| Age (average, SD) | $76.84(8.03)$ | $76.84(8.03)$ |
| Gender: Male | $6,037(56.17 \%)$ | $6,049(56.28 \%)$ |
| Race/Ethnicity | Whites | $3,301(30.71 \%)$ |
|  | Asian | $3,388(31.52 \%)$ |
|  | NHPI | $2,434(26.11 \%)$ |
| Other | $2,894(26.93 \%)$ |  |
| Dual Eligibility | $2,090(20.53 \%)$ | $2,316(21.55 \%)$ |
| Chronic Kidney Disease | $2,077(19.35 \%)$ | $2,215(20.0 \%)$ |
| Cataract | $4,390(40.84 \%)$ | $1,937(18.02 \%)$ |
| Chronic Obstructive Pulmonary Disease | $1,492(13.88 \%)$ | $1,521(14.02 \%)$ |
| Diabetes | $3,681(34.25 \%)$ | $3,566(33.18 \%)$ |
| Glaucoma | $1,889(17.58 \%)$ | $2,040(18.98 \%)$ |
| Hip/Pelvic Fracture | $113(1.05 \%)$ | $167(1.55 \%)$ |
| Depression | $953(8.87 \%)$ | $867(8.07 \%)$ |
| Osteoporosis | $1,397(13.00 \%)$ | $1,515(14.10 \%)$ |
| Rheumatoid Arthritis / Osteoarthritis | $2,719(25.30 \%)$ | $2,520(23.45 \%)$ |
| Anemia | $3,818(35.52 \%)$ | $3,882(36.12 \%)$ |
| Asthma | $1,028(9.56 \%)$ | $1,005(9.35 \%)$ |
| Hyperlipidemia | $6,351(59.09 \%)$ | $6,368(59.25 \%)$ |
| Hypertension | $6,867(63.89 \%)$ | $6,768(62.97 \%)$ |
| Acquired Hypothyroidism | $871(8.10 \%)$ | $765(7.12 \%)$ |
| Cancer Breast (among females) | $383(8.13 \%)$ | $373(7.93 \%)$ |
| Cancer Colorectal | $217(2.02 \%)$ | $247(2.30 \%)$ |
| Cancer Lung | $106(0.99 \%)$ | $85(0.79 \%)$ |
| Cancer Endometrial | $39(0.36 \%)$ | $71(0.66 \%)$ |
| Data | 2 |  |

Data are summarized using frequencies and percentages, unless specified otherwise.

Supplementary Table 5: A summary of subject characteristics among individuals with the initial event: ischemic heart disease (IHD), corresponds to the multistate model given in Fig. 1.

|  | Diseased set | Control |
| :--- | :--- | :--- |
| Total number of individuals | 12,781 | 12,781 |
| Age (average, SD) | $73.47(7.15)$ | $73.47(7.15)$ |
| Gender: Male | $7,810(61.11 \%)$ | $7,741(60.57 \%)$ |
| Race/Ethnicity | Whites | $4,246(33.22 \%)$ |
|  | Asian | $4,067(31.82 \%)$ |
|  | NHPI | $3,749(21.51 \%)$ |
| Other | $2,946(23.05 \%)$ |  |
| Dual Eligibility | $2,692(21.21 \%)$ | $3,144(24.60 \%)$ |
| Chronic Kidney Disease | $2,090(16.35 \%)$ | $2,294(20.53 \%)$ |
| Cataract | $1,591(12.45 \%)$ | $1,439(11.26 \%)$ |
| Chronic Obstructive Pulmonary Disease | $1,106(8.46 \%)$ | $3,732(29.20 \%)$ |
| Diabetes | $3,224(25.22 \%)$ | $1,281(10.02 \%)$ |
| Glaucoma | $1,611(12.60 \%)$ | $1,591(24.90 \%)$ |
| Hip/Pelvic Fracture | $67(0.52 \%)$ | $100(0.78 \%)$ |
| Depression | $825(6.45 \%)$ | $906(7.09 \%)$ |
| Osteoporosis | $1,094(8.56 \%)$ | $941(7.36 \%)$ |
| Rheumatoid Arthritis / Osteoarthritis | $2,171(16.99 \%)$ | $1,936(15.15 \%)$ |
| Anemia | $2,864(22.41 \%)$ | $2,941(23.01 \%)$ |
| Asthma | $942(7.37 \%)$ | $1,042(8.15 \%)$ |
| Hyperlipidemia | $6,009(47.02 \%)$ | $6,148(48.10 \%)$ |
| Hypertension | $6,279(49.13 \%)$ | $6,201(48.52 \%)$ |
| Acquired Hypothyroidism | $694(5.43 \%)$ | $510(3.99 \%)$ |
| Cancer Breast (among females) | $326(6.56 \%)$ | $361(7.16 \%)$ |
| Cancer Colorectal | $166(1.30 \%)$ | $120(0.94 \%)$ |
| Cancer Lung | $87(0.68 \%)$ | $125(0.98 \%)$ |
| Cancer Endometrial | $37(0.29 \%)$ | $19(0.15 \%)$ |

Data are summarized using frequencies and percentages, unless specified otherwise.

Supplementary Table 6: A summary of subject characteristics among individuals with the initial event: Stroke, corresponds to the multistate model given in Fig. 1.

|  | Diseased set | Control |
| :--- | :--- | :--- |
| Total number of individuals | 7,430 | 7,430 |
| Age (average, SD) | $76.4(7.48)$ | $76.4(7.48)$ |
| Gender: Male | $3,826(51.49 \%)$ | $3,763(50.65 \%)$ |
| Race/Ethnicity | Whites | $2,342(31.52 \%)$ |
|  | Asian | $2,230(30.02 \%)$ |
|  | NHPI | $1,890(25.44 \%)$ |
| Other | $1,002(26.94 \%)$ |  |
| Dual Eligibility | $1,284(18.63 \%)$ | $1,698(22.85 \%)$ |
| Chronic Kidney Disease | $1,377(18.99 \%)$ | $1,267(20.19 \%)$ |
| Cataract | $3,526(47.46 \%)$ | $1,294(17.41 \%)$ |
| Chronic Obstructive Pulmonary Disease | $1,057(14.23 \%)$ | $1,116(15.07 \%)$ |
| Diabetes | $2,596(34.94 \%)$ | $2,459(33.10 \%)$ |
| Glaucoma | $1,522(20.48 \%)$ | $1,635(22.00 \%)$ |
| Hip/Pelvic Fracture | $82(1.10 \%)$ | $100(1.35 \%)$ |
| Depression | $801(10.78 \%)$ | $735(9.89 \%)$ |
| Osteoporosis | $1,244(16.74 \%)$ | $1,235(16.62 \%)$ |
| Rheumatoid Arthritis / Osteoarthritis | $2,074(27.91 \%)$ | $1,933(26.01 \%)$ |
| Anemia | $2,791(37.56 \%)$ | $2,671(35.95 \%)$ |
| Asthma | $722(9.72 \%)$ | $818(11.01 \%)$ |
| Hyperlipidemia | $5,024(67.62 \%)$ | $4940(66.49 \%)$ |
| Hypertension | $4,770(64.2 \%)$ | $4,703(63.3 \%)$ |
| Acquired Hypothyroidism | $718(9.66 \%)$ | $828(11.15 \%)$ |
| Cancer Breast (among females) | $293(8.13 \%)$ | $249(6.78 \%)$ |
| Cancer Colorectal | $160(2.15 \%)$ | $189(2.55 \%)$ |
| Cancer Lung | $74(1.00 \%)$ | $61(0.82 \%)$ |
| Cancer Endometrial | $25(0.34 \%)$ | $37(0.50 \%)$ |

Data are summarized using frequencies and percentages, unless specified otherwise.

Supplementary Table 7: Estimated Occupational Probabilities for Developing AD and Death after Heart Disease and Stroke Conditions, Corresponds to Fig. 1.

|  |  | Model | Controls | Diseased Set |
| :---: | :---: | :---: | :---: | :---: |
| State - 0 | 48 Months | AF | 81.60(81.01,82.28) | 62.30(61.22,63.21) |
|  |  | AMI | 79.05(78.09,79.84) | 55.57(54.12,57.01) |
|  |  | HF | 85.18(84.32,85.92) | 57.60(56.51,58.70) |
|  |  | IHD | 86.27(85.51,86.90) | 74.48(73.47,75.25) |
|  |  | Stroke | 81.14(80.07,82.05) | 71.37(70.28,72.53) |
|  | 96 Months | AF | 59.37(58.10,60.76) | 40.57(39.05,42.21) |
|  |  | AMI | 54.76(52.99,56.70) | 35.44(33.79,37.16) |
|  |  | HF | 64.76(63.27,66.11) | 35.03(33.29,36.61) |
|  |  | IHD | 68.45(66.81,69.76) | 56.73(55.10,58.11) |
|  |  | Stroke | 57.91(56.06,59.75) | 50.18(48.53,51.86) |
| State - 1 | 48 Months | AF | 1.32(1.11,1.55) | 1.08(0.89,1.31) |
|  |  | AMI | 1.43(1.13,1.69) | 1.09(0.82,1.31) |
|  |  | HF | 1.30(1.05,1.57) | 1.07(0.80,1.28) |
|  |  | IHD | 0.88(0.70,1.04) | 0.98(0.79,1.23) |
|  |  | Stroke | 1.32(1.03,1.64) | 1.49(1.16,1.77) |
|  | 96 Months | AF | 2.29(1.87,2.78) | 1.48(1.14,1.98) |
|  |  | AMI | $2.17(1.61,2.85)$ | 1.29(0.71,1.97) |
|  |  | HF | 2.20 (1.74,2.70) | 0.95(0.54,1.49) |
|  |  | IHD | 1.81(1.30,2.35) | 1.22(0.56,1.80) |
|  |  | Stroke | 1.97(1.43,2.53) | $2.34(1.56,3.06)$ |
| State - 2 | 48 Months | AF | 17.14(16.46,17.79) | 36.63(35.73,37.61) |
|  |  | AMI | 19.59(18.81,20.58) | 43.40(41.99,44.91) |
|  |  | HF | 13.59(12.85,14.36) | 41.35(40.13,42.46) |
|  |  | IHD | 12.86(12.20,13.56) | 24.56(23.76,25.53) |
|  |  | Stroke | 17.57(16.66,18.54) | 27.16(25.99,28.17) |
|  | 96 Months | AF | 38.38(37.11,39.52) | 58.05(56.42,59.53) |
|  |  | AMI | 43.07(41.10,44.83) | 63.27(61.69,65.03) |
|  |  | HF | 33.09(31.53,34.74) | 64.01(62.25,65.82) |
|  |  | IHD | 29.74(28.40,31.23) | 42.04(40.69,43.86) |
|  |  | Stroke | 40.12(38.22,41.99) | 47.49(45.73,49.33) |

Table shows estimated state occupational probabilities and $95 \%$ confidence inter-vals for developing AD and death after heart disease and stroke, corresponding to Fig. 1.

Supplementary Table 8: Effects of the dual eligibility indicator on transitions in the multistate model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR $(95 \% \mathrm{CI})$ | p | RR $(95 \% \mathrm{CI})$ | p | RR $(95 \% \mathrm{CI})$ | p |
| AF | $1.628(1.277,2.075)$ | $<0.0001$ | $1.072(0.865,1.328)$ | 0.5244 | $1.419(1.195,1.685)$ | $<0.0001$ |
| AMI | $3.948(2.025,7.696)$ | $<0.0001$ | $1.349(1.038,1.753)$ | 0.0252 | $1.272(1.129,1.433)$ | $<0.0001$ |
| HF | $1.463(1.093,1.958)$ | 0.0105 | $0.977(0.588,1.623)$ | 0.9284 | $1.113(1.033,1.199)$ | 0.0047 |
| IHD | $1.962(1.404,2.742)$ | $<0.0001$ | $1.766(1.329,2.347)$ | $<0.0001$ | $1.447(1.203,1.740)$ | $<0.0001$ |
| Stroke | $1.391(1.054,1.836)$ | 0.0197 | $1.397(1.027,1.901)$ | 0.0334 | $1.311(1.144,1.502)$ | $<0.0001$ |

The table presents the effects of the dual eligibility indicator on transitions in the multistate model shown in Fig. 2, by the risk ratio (RR). The estimated RR values correspond to the effect of the dual-eligible cohort compared to the Medicare-only cohort.

Supplementary Table 9: Effects of the gender on transitions in the multistate model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR (95\% CI) | p | RR (95\% CI) | p | $\mathrm{RR}(95 \% \mathrm{CI})$ | p |
| AF | $0.808(0.653,1.000)$ | 0.0496 | $0.868(0.758,0.993)$ | 0.0397 | $1.076(1.021,1.134)$ | 0.0064 |
| AMI | $0.484(0.322,0.728)$ | 0.0005 | $1.208(0.983,1.484)$ | 0.0718 | $0.981(0.911,1.056)$ | 0.6093 |
| HF | $0.748(0.584,0.958)$ | 0.0216 | $0.988(0.680,1.434)$ | 0.9494 | $1.202(1.098,1.316)$ | $<0.0001$ |
| IHD | $0.645(0.518,0.803)$ | $<0.0001$ | $1.584(1.152,2.177)$ | 0.0046 | $1.080(1.023,1.140)$ | 0.005 |
| Stroke | $0.802(0.624,1.031)$ | 0.0852 | $1.268(0.965,1.667)$ | 0.0888 | $1.309(1.143,1.499)$ | $<0.0001$ |

The table presents the effects of the gender on transitions in the multistate model shown in Fig. 2, by the risk ratio (RR). The estimated RR values correspond to the effect of males compared to females.

Supplementary Table 10: Effects of the age variable on transitions in the multistate model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR $(95 \%$ CI $)$ | p | RR $(95 \%$ CI $)$ | p | RR $(95 \%$ CI $)$ | p |
| AF | $1.089(1.044,1.136)$ | $<0.0001$ | $1.032(1.016,1.048)$ | $<0.0001$ | $1.055(1.028,1.083)$ | $<0.0001$ |
| AMI | $1.110(1.054,1.169)$ | $<0.0001$ | $1.068(1.034,1.103)$ | $<0.0001$ | $1.056(1.028,1.085)$ | $<0.0001$ |
| HF | $1.088(1.044,1.134)$ | $<0.0001$ | $1.038(1.011,1.066)$ | 0.0063 | $1.040(1.020,1.060)$ | $<0.0001$ |
| IHD | $1.109(1.054,1.167)$ | $<0.0001$ | $1.039(1.019,1.059)$ | 0.0001 | $1.059(1.029,1.090)$ | $<0.0001$ |
| Stroke | $1.102(1.050,1.157)$ | $<0.0001$ | $1.035(1.015,1.056)$ | 0.0006 | $1.060(1.030,1.091)$ | $<0.0001$ |

The table presents the effects of the age variable on transitions in the multistate model shown in Fig. 2, by the risk ratio (RR). The estimated $R R$ values correspond to the effect age by a unit (i.e., years) increment.

Supplementary Table 11: Effects of Chronic Kidney Disease history on transitions in the multistate model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR (95\% CI) | p | RR $(95 \% \mathrm{CI})$ | p | $\mathrm{RR}(95 \%$ CI) | p |
| AF | $1.006(0.997,1.015)$ | 0.1672 | $3.271(1.469,7.282)$ | 0.0037 | $1.867(1.381,2.524)$ | $<0.0001$ |
| AMI | $1.000(0.986,1.015)$ | 0.9701 | $3.859(1.924,7.741)$ | 0.0001 | $1.691(1.312,2.180)$ | $<0.0001$ |
| HF | $0.993(1.005,0.981)$ | 0.2706 | $1.604(0.961,2.677)$ | 0.0706 | $1.432(1.010,2.031)$ | 0.0441 |
| IHD | $0.990(0.981,0.998)$ | 0.0203 | $1.580(0.9852 .535)$ | 0.0580 | $1.722(1.324,2.239)$ | $<0.0001$ |
| Stroke | $0.998(0.987,1.009)$ | 0.7279 | $1.503(0.816,2.769)$ | 0.1909 | $1.628(1.286,2.061)$ | $<0.0001$ |

The table presents the effects of the Chronic Kidney Disease history on transitions in the multistate model shown in Fig. 2, by the risk ratio (RR).

Supplementary Table 12: Effects Diabetes history on transitions in the multistate model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR (95\% CI) | p | RR (95\% CI) | p | RR (95\% CI) | p |
| AF | $1.005(0.996,1.014)$ | 0.2559 | $1.767(1.067,2.926)$ | 0.0270 | $1.418(1.198,1.679)$ | $<0.0001$ |
| AMI | $1.007(0.993,1.022)$ | 0.3244 | $1.292(0.961,1.737)$ | 0.0898 | $1.354(1.166,1.572)$ | $<0.0001$ |
| HF | $1.122(1.001,1.257)$ | 0.0474 | $1.652(0.958,2.849)$ | 0.0711 | $1.298(0.938,1.797)$ | 0.1160 |
| IHD | $1.098(1.001,1.205)$ | 0.0482 | $1.295(0.900,1.864)$ | 0.1643 | $1.477(1.217,1.793)$ | $<0.0001$ |
| Stroke | $0.991(0.979,1.004)$ | 0.1577 | $1.565(1.080,2.268)$ | 0.0180 | $1.561(1.2471 .954)$ | $<0.0001$ |

The table presents the effects of the Diabetes history on transitions in the multi-state model shown in Fig. 2, by the risk ratio ( RR ).

Supplementary Table 13: Effects of Hypertension history on transitions in the multistate model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR $(95 \%$ CI $)$ | p | RR $(95 \%$ CI $)$ | p | $\operatorname{RR}(95 \% \mathrm{CI})$ | p |
| AF | $1.089(0.993,1.194)$ | 0.0704 | $0.940(0.871,1.014)$ | $<0.1101$ | $1.075(0.993,1.164)$ | 0.0753 |
| AMI | $1.109(0.973,1.265)$ | 0.1225 | $0.967(0.908,1.030)$ | 0.2990 | $1.095(0.877,1.368)$ | 0.4238 |
| HF | $1.195(1.028,1.389)$ | 0.0204 | $0.923(0.472,1.804)$ | 0.8150 | $1.211(1.064,1.378)$ | 0.0037 |
| IHD | $1.181(1.027,1.357)$ | 0.0192 | $0.993(0.982,1.004)$ | 0.2196 | $1.088(0.890,1.330)$ | 0.4108 |
| Stroke | $0.995(0.986,1.003)$ | 0.2231 | $0.819(0.645,1.039)$ | 0.1002 | $0.994(0.970,1.018)$ | 0.6221 |

The table presents the effects of the Hypertension history on transitions in the multistate model shown in Fig. 2, by the risk ratio (RR).

Supplementary Table 14: Effects of Hyperlipidemia history on transitions in the multi-state model, given in Fig. 2.

|  | State-0 to State-1 |  | State-1 to State-2 |  | State-0 to State-2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RR (95\% CI) | p | RR (95\% CI) | p | RR (95\% CI) | p |
| AF | $1.000(0.992,1.008)$ | 0.9510 | $1.161(0.748,1.801)$ | 0.5066 | $0.842(0.643,1.102)$ | $<0.2101$ |
| AMI | $0.985(0.969,1.001)$ | 0.0725 | $0.621(0.280,1.378)$ | 0.2411 | $0.828(0.625,1.097)$ | $<0.1891$ |
| HF | $0.994(0.985,1.003)$ | 0.2017 | $1.511(0.943,2.421)$ | 0.0860 | $1.025(0.984,1.067)$ | 0.2358 |
| IHD | $0.897(0.880,1.005)$ | 0.3621 | $1.003(0.997,1.009)$ | 0.3407 | $0.861(0.684,1.084)$ | $<0.2022$ |
| Stroke | $1.006(0.997,1.014)$ | 0.2119 | $0.745(0.546,1.018)$ | 0.0648 | $0.876(0.674,1.138)$ | $<0.3214$ |

The table presents the effects of the Hyperlipidemia history on transitions in the multistate model shown in Fig. 2, by the risk ratio (RR).

Supplementary Table 15: Results of a sensitivity analysis conducted on transitioning from heart disease and stroke to AD (State 0 to 1, Fig. 1) using the Fine and Gray competing risk approach.

|  | HR | p |
| :---: | :---: | :---: |
| AF | 1.152 | $<0.0001$ |
| AMI | 1.125 | 0.0352 |
| HF | 1.161 | $<0.0001$ |
| IHD | 1.204 | $<0.0001$ |
| Stroke | 1.168 | $<0.0001$ |

The estimated hazard ratio (HR) values correspond to the effect of the disease groups (i.e., AF, AMI, HF, IHD, and stroke) compared to the control group.

Supplementary Table 16: Results of a sensitivity analysis conducted on transitioning from heart disease and stroke to AD (State 0 to 1, Fig. 2) using the Fine and Gray competing risk approach: Racial/ethnic effects.

|  |  |  | NHPI vs. Whites |  | NHPI vs. Asians |  | Asians vs. Whites |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | HR | p | HR | p | HR | p |  |
|  | AF | 0.856 | 0.0701 | 0.895 | 0.1112 | 0.956 | 0.7863 |  |
|  | AMI | 0.971 | 0.9045 | 1.154 | 0.5521 | 0.841 | 0.1245 |  |
|  | HF | 0.686 | 0.0208 | 0.581 | $<0.0001$ | 1.181 | 0.1265 |  |
|  | IHD | 0.721 | 0.0544 | 0.587 | $<0.0001$ | 1.228 | 0.0504 |  |
|  | Stroke | 0.979 | 0.2502 | 0.905 | 0.6211 | 1.082 | 0.8626 |  |
|  | AF | 1.023 | 0.8022 | 1.615 | 0.0004 | 0.633 | $<0.0001$ |  |
|  | AMI | 0.939 | 0.4025 | 1.578 | 0.0121 | 0.595 | $<0.0001$ |  |
|  | HF | 1.445 | 0.0121 | 1.805 | $<0.0001$ | 0.801 | 0.0301 |  |
|  | IHD | 1.155 | 0.0675 | 1.855 | $<0.0001$ | 0.623 | $<0.0001$ |  |
|  | Stroke | 1.388 | 0.0192 | 1.951 | $<0.0001$ | 0.711 | 0.0458 |  |

The table summarizes the race/ethnicity-based hazard ratio (HR) values observed in the transition from state 0 to state 1 in the multistate model presented in Fig. 2.

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