Ultrasound breast images denoising using generative adversarial networks (GANs)

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Abstract.

INTRODUCTION: Ultrasound in conjunction with mammography imaging, plays a vital role in the early detection and diagnosis of breast cancer. However, speckle noise affects medical ultrasound images and degrades visual radiological interpretation. Speckle carries information about the interactions of the ultrasound pulse with the tissue microstructure, which generally causes several difficulties in identifying malignant and benign regions. The application of deep learning in image denoising has gained more attention in recent years.

OBJECTIVES: The main objective of this work is to reduce speckle noise while preserving features and details in breast ultrasound images using GAN models.

METHODS: We proposed two GANs models (Conditional GAN and Wasserstein GAN) for speckle-denoising public breast ultrasound databases: BUSI, DATASET A, AND UDIAT (DATASET B). The Conditional GAN model was trained using the Unet architecture, and the WGAN model was trained using the Resnet architecture. The image quality results in both algorithms were measured by Peak Signal to Noise Ratio (PSNR, 35–40 dB) and Structural Similarity Index (SSIM, 0.90–0.95) standard values.

RESULTS: The experimental analysis clearly shows that the Conditional GAN model achieves better breast ultrasound despeckling performance over the datasets in terms of PSNR = 38.18 dB and SSIM = 0.96 with respect to the WGAN model (PSNR = 33.0068 dB and SSIM = 0.91) on the small ultrasound training datasets.

CONCLUSIONS: The observed performance differences between CGAN and WGAN will help to better implement new tasks in a computer-aided detection/diagnosis (CAD) system. In future work, these data can be used as CAD input training for image classification, reducing overfitting and improving the performance and accuracy of deep convolutional algorithms.

Keywords: Breast cancer, ultrasound image denoising, generative adversarial network

1. Introduction

Medical image analysis plays an important role in breast cancer screening, feature extraction, segmentation, and classification breast lesions locally. There are several breast cancer detection methods, such as

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Positron Emission Tomography (PET) [1], Computer Tomography (CT) [2] and Magnetic Resonance Imaging (MRI) [3], which are usually used when women are at high risk of breast cancer. Other complementary techniques such as X-ray mammography [4] and ultrasound (US) [5] are more commonly used in screening programs, according to the American Cancer Society.

Among these modalities, US is used as a complementary imaging modality for further evaluation of lesions detected early by mammography due to its non-invasive nature, low cost, safety, portability, and low radiation dose. However, one of its main shortcomings is the poor quality of US image, which is corrupted by random noise added during its acquisition [6,7], i.e. low contrast and different brightness levels, resulting in increased noise and artifacts that can affect the radiologist's opinion and diagnosis. US images have a granular appearance called speckle noise, which degrades visual assessment [8], making it difficult for humans to distinguish normal from pathological tissue in diagnostic examinations.

Image denoising techniques, typically low-dose, address this problem [9]. The primary purpose of denoising is to restore the maximum detail of the image by removing excess noise [10], while preserving as much as possible the feature details to benefit the diagnosis and classification of benign, premalignant, and malignant abnormalities (microcalcifications, masses, nodules, tumors, cysts, fibroadenoma, adenosis, and lesions) that may be difficult to identify at first sight or early in the patient.

Thus, denoising medical images is essential before training a classifier based on deep-learning models. Recently, several US denoising techniques based on deep learning have been widely used, such as Convolutional Neural Networks (CNN) [11,12,13,14], Generative Adversarial Networks (GANs) [15, 16,17], and Autoencoders (AEs) [18,19], which can recover the original dataset and make it noise-free with better robustness and precision [20]. Deep learning methods have obtained better results in medical imaging in comparison with previous methods such as Wavelet, Wiener, Gaussian [21], Multi-Layer perceptron [22], Dictionary Learning [23], Least Square, Bilateral Filter, Non-Local Mean [24]. Variational approaches [6,25], because these filters have presented some limitations such as smoothing problems, more computational cost, and inability to preserve information such as edges and textures of images as well as possible [25].

2. Related work

Many traditional denoising filtering techniques have been proposed in the literature to reduce speckle noise [26,27,28,29], which can be categorized into three main types: 1) Spatial domain (Median filter, Mean filter, Adaptive Mean Filter, Frost, Total variation filter, Anisotropic Diffusion, Nonlocal means filter, Linear Minimum Mean Squared Error (LMMSE)). 2) Transform domain (Wiener filter, Low pass filter, Discrete wavelet transform), and 3) Deep learning-based techniques such as Convolutional Neural Networks (CNN), Generative Adversarial Networks (GAN), and Variational Autoencoders (VAEs).

The Spatial and Transform domain methods are computationally simple and fast but sometimes blur the image, and there can be a loss of resolution and low accuracy. Spatial domain filters also have size limitations and window shape problems [28].

However, Deep learning-based models can provide better results compared to these traditional methods, because deep models gives better visual quality by extracting various features of an image as example Li et al. proposed TP-Net [30] as 3D shape classification and segmentation tasks, on a wide range of common datasets, which main contribution is the design of dilated convolution strategy tailored for the irregular and non-uniform structure of 3D mesh data.

Several Generative models (GANs, VAEs) have been successfully used for medical image denoising and data augmentation to improve robustness and prevent overfitting in deep CNN image classification algorithms. Some relevant works are discussed in this section.

Wu et al. [31] implemented a perceptual metrics-guided GAN (PIGGAN) framework to intrinsically optimize generation processing, and experiments show that PIGGAN can produce photo-realistic results and quantitatively outperforms state-of-the-art (SOTA) methods. Pang et al. [32] implemented the TripleGAN model to augment the breast US images. These synthetic images were used to classify breast masses classification using the CNN model, achieving a classification accuracy of 90.41%, sensitivity of 87.94% and specificity of 85.86%. Al-Dhabyani et al. [33] first used breast US data augmentation with GAN and then two deep learning classification approaches: (i) CNN (AlexNet) and (ii) TL (VGG16, ResNet, Inception, and NASNet), achieving in the BUSI dataset an accuracy of 73%, 84%, 82%, 89%, 91% and in Dataset B (UDIAT) an accuracy of 75%, 80%, 77%, 86%, 90% respectively.

Jain et al [34] found that CNN provided comparable and, in some cases, superior performance to Wavelet and Markov Random Field methods. Thus, the Resnet approach proposed by MRDG et al. [11] was used to improve mammography image quality with a peak signal-to-noise ratio (PSNR) of 36.18 and a similar structural index metrix (SSIM) of 0.841. Feng et al [13] implemented a hybrid neural network for US denoising based on the Gaussian noise distribution and VGGNet model to extract the structural boundary information, the results show a (PSNR = 30.57, SSIM = 0.90, Mean Square Error (MSE) = 66.61) US denoising effectiveness.

Denoising autoencoders based on convolutional layers also perform well for their ability to extract spatial solid correlation [35]. Kaji et al. [9] present an overview describing encoder-decoder networks (pix-2-pix) and cycle GAN as image noise reduction.

Chen et al. [12] proposed the autoencoder and the residual encoder–decoder CNN for low-dose computer tomography (CT) imaging, achieving a good performance index (PSNR of 39.19/SSIM of 0.93 and Root Mean Square Deviation (RMSD) of 0.0097), compared to with other methods in terms of noise suppression, structure preservation, and lesion detection.

However, the use of GANs is considered more stable than autoencoders. GANs are typically used when dealing with images or visual data and work better for signal image processing, such as anomaly detection; on the contrary, VAEs are used for predictive maintenance or security analysis applications [35]. For the previous reason, several GANs have recently been used for data augmentation [36,37,38,39,40], image super-resolution [21], image translation [9], and noise reduction in the medical field [41,42].

Zhou et al. [37] proposed a GAN + U-Net network (generator model) to achieve mapping between low-quality US images and corresponding high-quality images. In contrast to the traditional GAN method, U-Net is used to reconstruct the image's tissue structure, details, and speckles. The evaluation indices indicated that PSNR, SSIM, and MI (Mutual dependence index) values are increased by 48.3%, 205.0%, and 44.0% and that the proposed method can successfully reconstruct a high-quality image.

The most recent deep GAN models used for image denoising are Conditional GAN [43] and Wasserstein GAN [44], which have shown better performance than conventional denoising algorithms [45,46]. Kim et al. [43] implemented a CGAN network as a medical image denoising algorithm, where the SSIM metric was improved by 1.5 and 2.5 times over conventional methods (Nonlocal Means and Total Variation) respectively, demonstrating a superiority in quantitative evaluation. Vimala et al. [47] proposed an image noise removal in US breast images based on Hybrid Deep Learning Technique, where local speckle noise was destroyed, reaching a signal-to-noise ratios (SNRs) greater than 65 dB, PSNR ratios greater than 70 dB, edge preservation index values more significant than the experimental threshold of 0.48. Zou et al. [37] proposed a network model based on the Wasserstein GAN for image denoising, which improved the noise removal effect.

Based on the previous mentioned our propose integrates concepts from breast cancer research and ultrasound image denoising in a comparative study to evaluate the effect of image pre-processing in

Dataset Benign Malignant Total BUSI 437 210 647 Dataset A 100 150 250 Dataset B 110 53 163 Total 647 413 1060

Table 1
Breast ultrasound public databases

improving breast image quality. Improving image quality clarifies patterns, allowing the deep learning model to identify and classify features within the image more accurately. In this study, we explore a novel approach by combining fine-tuning techniques GANs + CNNs, providing new insights into breast cancer classification.

Denoising of medical images has been used to improve the performance of CNN segmentation and classification algorithms [48,50]. Ans several CNN methods for general image denoising have been studied ADNet, NERNet, SAnet, CDNet, DRCNN [51], but in this research, as a technical novelty, we combine Conditional GAN + Unet and WGAN + Resnet particularly focusing on the medical image quality improvement of breast ultrasound. The results will help to better implement new tasks in a computer-aided detection/diagnosis (CAD) system.

Consenquently, this study aims to: (i) to implement two types of GANs+CNNs architecture models as speckle denoising in ultrasound breast images, and (ii) to select the best architecture to generate new quality images based on the quantitative evaluation metrics (PSNR and SSIM).

3. Materials and methods

3.1. Databases collection

Three publicly available breast US databases were used in this study: (i) The *Breast Ultrasound Images Dataset (BUSI*, https://scholar.cu.edu.eg/?q=afahmy/pages/dataset) [52]. This contains data from 600 female patients. The dataset consists of 780 images (133 normal, 437 benign and 210 malignant) with an average image size of 500×500 pixels. (ii) The *Dataset A* is obtained from Rodrigues et al. [53] (https://data.mendeley.com/datasets/wmy84gzngw/1) and contains 250 breast cancer images, 100 benign and 150 malignant. The *Dataset B* (Breast Ultrasound Lesions Dataset, http://www2.docm.mmu. ac.uk/STAFF/m.yap/dataset.php) collected in UDIAT-Centre Diagnóstic, Corporació Parc Taulí, Sabadell (Spain). The dataset consists of 163 images of different women with an average image size of 760×570 pixels, each of the images shows one or more lesions. Of the 163 images of lesions, 53 are images of cancerous masses and 110 with benign lesions [54].

A total of 1060 US images were used to train the GAN models; see Table 1.

Figure 1 shows the workflow used in denoising breast ultrasound images, which is divided into the following steps: i) Acquisition of public ultrasound databases, ii) Dimensionality and cropping of regions of interest (RoIs), iii) Image denoising using two GANs + CNN models, and iv) Image quality evaluation.

3.2. Data dimensionality and rois cropping

The torchvision (pytorch) library was used to perform transformations (preserving all features and structure of the images) and to standardize the images to a single dimension (256×256 pixels), which

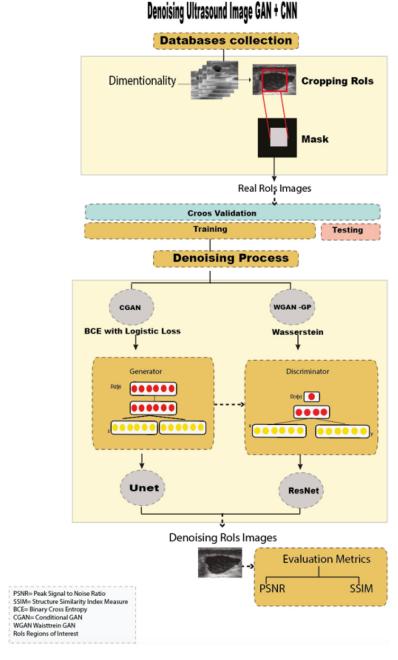


Fig. 1. Workflow of GANs+CNN models implementation in breast ultrasound denoising.

were acquired in different sizes (BUSI: 431×476 , 765×590 , 786×556 ; Dataset A: 153×87 , 95×75 , 93×57 ; Dataset B: 760×570).

According to Wu et al. [36], synthesizing a lesion into RoIs (regions of interest) gives advantages to the generative model, as it generates more realistic lesions, improving subsequent classification performance over traditional augmentation techniques. Thus, automatic RoI extraction was performed on all US

images.

Then, using a cross-validation technique, the dataset was randomly divided (with the Sklearn library) into a training set (80%, 851 images) and a testing set (20%, 209 images) for training the GAN models (with the Tensorflow, Keras libraries).

3.3. Generative adversarial network

The GAN architecture is represented by a generative (G) network and a discriminator (D) network, which are trained simultaneously. While the G network is trained to produce realistic images G(z) from a random vector z, the D network is trained to discriminate between real and generated images [55]. In the original GAN the optimization function was formulated by the Eq. (1).

$$min_{G}max_{D} V(D,G) = E_{x \sim P_{r(x)}} [\log D(x)] + E_{z \sim P_{z}(z)} [\log (1 - D(G(z)))]$$
 (1)

Given random noise vector z and real image x, the generator attempts to minimize $\log (1 - D(G(z)))$ and the discriminator attempts to maximize $\log D(x)$. Whre, P_r and P_z sare the real data distribution and the noise data distribution, x is the input variable, D(x) is the prediction label and D(z) is the generated sample.

In this work, we used two ultrasound denoising GANs; (i) conditional GAN and (ii) WGAN, both has been widely used in medical image reconstruction, denoising and data augmentation [56]. Especially CGAN model have been propose as new framework that can largely mitigate the biases and discriminations in machine learning systems while at the same time enhancing the prediction accuracy of these systems [57].

3.3.1. Conditional GAN (CGAN)

CGAN was introduced by Douzas et al. [58], as an extension of GAN with conditional information in D and G. GANs are generative models that learn a mapping from random noise vector z to output image y, $(G: z \to y)$ [59]. In contrast, conditional GANs learn a mapping from observed image x and random noise vector z to y, $(G: \{x, z\} \to y)$. The CGAN objective function is framed by Eq. (2), where G tries to minimize this objective function and D tries to maximize it.

$$L_{cGAN}(G, D) = E_{x,y} \left[\log D(x, y) \right] + E_{x,z} \left[\log(1 - D(x, G(x, z))) \right]$$
(2)

In this work, the generator and discriminator architectures were adapted from [60,61]. A manual exploration of different configurations in the general hyperparameters was performed to optimize the denoising of breast US images, before selecting and implementing our CGAN model. The selected hyperparameters are: Number of epochs = 40, Buffer size = 954, Batch size = 80; Optimiser = Adam, Activation function = Binary Cross-Entropy Loss, Generator layers = 48 and Discriminator layers = 12. The *denoiser generator* network is based on the U-Net [61] architecture, which consists of a contraction path and an expansion path. This is composed of 48 convolutional layers including the input layer, 8 contraction layers, 7 expansion layers, 6 concatenation layers spread over the expansion layers, and finally a transposed convolutional layer. Each encoder and decoder block is replaced by residual dense connectivity and batch normalization to remove speckle noise followed by the ReLU function (Fig. 2, Appendix S.1 and S.2).

The *denoiser discriminator* network is based on a Markovian random field (PatchGAN). This consists of an input convolutional layer and 24 convolutional layers followed by batch normalization and a ReLU function (Fig. 2). The output consists of successive convolutional layers 256, 128, 64 and 1. This means that as the input image passes through each of the convolution blocks, the spatial dimension is reduced by a factor of two.

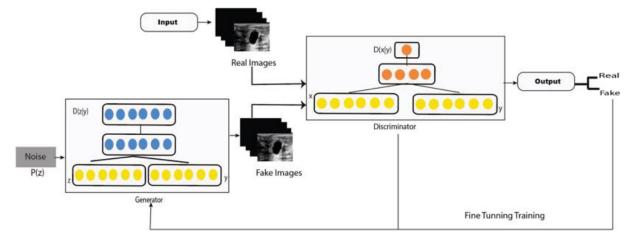


Fig. 2. CGAN model.

3.3.2. Wasserstein GAN (WGAN)

WGAN was introduced by Arjovsky et al. [62], which uses a Wasserstein distance instead of a JS (Jensen-Shanon) or KL (Kullback-Leibler) divergence to evaluate the discrepancy between the distribution distance of noisy and denoised images. It provides a better approximation of the distribution of the observed data in the training data.

The Wassertein (W) model is defined as Eq. (3):

$$W(P_r, P_g) = \inf_{\gamma} \sim \Pi(P_r, P_g) \operatorname{E}(x, y) \sim \gamma ||x - y||$$
(3)

Where $\Pi\left(P_r,P_g\right)$ denotes the set of all the joint distributions $\gamma\left(x,y\right)$ based on the marginal values of P_r and P_g ; $\gamma\left(x,y\right)$ indicates how many "RoIs" must be transported from x to y in order to transform the distributions P_r into the distribution P_g ; x and y denote the predicted and real actual values, respectively, and P denotes the probability distribution. The general hyperparameters implemented in this model are number of epochs = 130, buffer size = 954, batch size = 60; optimizer = Adam, octivation function = Wasserstein, generator layers = 26 and discriminator layers = 12.

The denoising generator, was trained by the Resnet model [63]. The generator contains 54 layers, including the input layer, 8 sequential layers of 3 layers each (convolutional layer, normalisation layer and LeakyReLU layer), 7 residual sequences of 4 layers each (transposed convolutional layer, normalisation layer, dropout layer and LeakyReLU layer) and finally a transposed convolutional layer (Fig. 3, Appendix S.3 and S.4).

The *denoising discriminator* uses the PatchGAN model combined with the Res-Net architecture (convolutional layer, normalization layer and LeakyReLU layer), where the layers were connected directly in a single sequence instead of linking several sequences.

The training phase was carried out with the Google Colab GPU PRO environment, using the Tensorflow and Sklearn libraries for image pre-processing, and PyTorch (CUDA 10.2 graphics cores) to obtain more computational resources and minimise the algorithm execution time. The Tensorflow and Keras libraries were used to train the GAN models.

3.4. Evaluation metrics

In addition, most filter techniques use various evaluation metrics such as Mean Square Error (MSE), Root-Mean-Square Error (RMSE), Signal-to-Noise Ratio (SNR), Peak Signal-to-Noise Ratio (PSNR) and Structural Similarity Index (SSIM) to assess image quality.

Table 2 PSNR and SSIM range values

Quality	PSNR	SSIM
Low	< 30	< 0.90
Aceptable	35-40	0.90 – 0.95
High	40-50	0.95-1

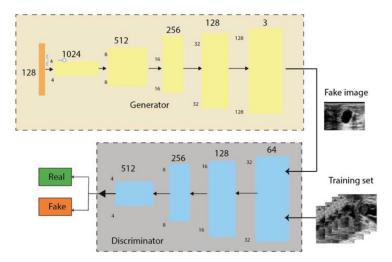


Fig. 3. WGAN model. Adapted from Hao, Zhuangzhuang et al. (2022).

For quantitative comparison, the PSNR and SSIM [64,65] were introduced to measure image restoration quality, which is widely used in biomedical applications, especially in mammography and US diagnosis and cancer detection fields.

The PSNR is the metric used to measure the quality of the denoising image when it is corrupted due to noise and blur. A higher value of PSNR indicates a higher quality rate. The standard value of PSNR is 35 to 40 dB (Table 2). The PSNR is calculated by Eq. (4), where is the variance of noise evaluated over the RoI image and is the variance of the filtered image.

$$PSNR = 10 \log \left(\frac{\sigma_s^2}{\sigma_{\hat{s}}} \right) \tag{4}$$

SSIM is a perception-based model that considers the image degradation as perceived change in contrast and structural information. Thus, we can apply this value to assess the quality of any images [66], which lies from 0 to 1 (Table 2).

SSIM index is computed using the correlation coefficient, see Eq. (5).

$$SSIM(x,y) = \frac{(2\mu_x + \mu_y)(2\sigma_{xy})}{(\mu x^2 + \mu y^2)(\sigma x^2 + \sigma y^2)}$$
 (5)

Where.

$$u_x = \frac{1}{N} \sum_{i}^{N} = 1x_i$$

$$u_y = \frac{1}{N} \sum_{i}^{N} = 1y_i$$

ID **CGAN** ID WGAN PSNR (dB) SSIM PSNR (dB) SSIM **BUSI** 39.8433 0.974624 35.0476 0.930708 img_busi _7 img_busi_7 img_busi_56 39.8223 0.906241 img_busi_56 35.1609 0.818753 39.8341 img_busi _58 0.976325 img_busi_58 35.5627 0.952616 img_busi_60 0.978979 35.2361 40.1839 img_busi_60 0.931421 img_busi _70 39.7809 0.971730img_busi_70 35.7736 0.943916 img_busi_175 39.4099 0.972768 img_busi_175 35.5431 0.942358 img_busi _199 39.7116 0.929269 img_busi_199 35.3159 0.939286 DATASET A 0.977663 img_datasetA_6 41.8245 img_datasetA_6 38.2882 0.965505 img_datasetA_11 42.1565 0.977758 37.7888 0.965114 img_datasetA_11 img_datasetA_23 41.8171 0.978695 img_datasetA_23 38.2925 0.967823 38.4245 img_datasetA_76 41.9047 img_datasetA_76 0.977636 0.971207 img_datasetA_188 41.9888 0.977348 37.2507 0.968667 img_datasetA_188 img_datasetA_217 41.9424 0.978819 img_datasetA _217 37.7399 0.971379 img_datasetA_222 42.6280 0.980217 img_datasetA_222 37.2250 0.967832 UDIAT img_udiat_55 38.0735 0.876853 img_udiat_55 34.1079 0.936932 img_udiat_77 40.4911 0.967255 img_udiat_77 36.4130 0.939990 img_udiat_102 36.9104 0.967851 img_udiat_102 34.5283 0.932152 img_udiat_114 36.8855 0.967821 img_udiat_114 34.1357 0.930100 img_udiat_135 36.9244 0.972911 img_udiat_135 33.3826 0.939381 img_udiat_165 38.8622 0.967638 img_udiat_165 34.3925 0.922628

0.961544

0.961547

img_udiat_200

Total average

33.7251

33.0068

0.918583

0.919955

Table 3
Summary of the CGAN and WGAN average comparison results (PSNR and SSIM)

$$\sigma_{x} = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (x_{i} - \mu_{x})^{2}}$$

$$\sigma_{y} = \sqrt{\frac{1}{N-1} \sum_{i=1}^{N} (y_{i} - \mu_{y})^{2}}$$

$$\sigma_{xy} = \frac{1}{N-1} \sum_{i=1}^{N} (x_{i} - \mu_{x}) (y_{i} - \mu_{y})$$

37.9759

img_udiat_200

Total average

N is the total number of pixels in the image. $x_{i,j}$ is the filtered image at i and j coordinates and $y_{i,j}$ is the noisy image at i and j coordinates. μ_x μ_I is the mean of reference images, μ_y μ_i is the mean of filtered images, σ_x is the variance of reference images, σ_y is the variance of filtered image, $\cot y_i \cot y_j$ is the covariance of filtered image.

4. Results

This section presents the most relevant numerical experiments obtained from speckle removal GAN algorithms. First, to improve the algorithm performance, the RoI images were used as GAN training models; in total, we denoising 1060 malignant and benign RoIs. The image quality of the generated

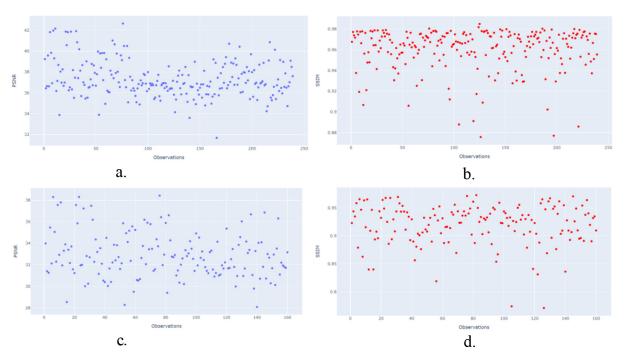


Fig. 4. Dispersion report for PSNR/SSIM metrics. a). CGAN network with PSNR metric. b). CGAN network with SSIM metric. c). WGAN network with PSNR metric. d). WGAN network with SSIM metric.

data was evaluated with PSNR and SSIM metrics, which are expressed in terms of average value. The most relevant scores are displayed in Table 3; these indicate that the Conditional GAN model showed a significant improvement compared to the other model.

Although they are visually very similar according to Table 4, the quality values obtained define that the CGAN network achieves a higher mean value in PSNR = 41.03 dB and SSIM = 0.97 concerning the WGAN network values (PSNR = 35.47 dB/SSIM = 0.43). This indicates that the CGAN model is the network that best eliminates the speckle noise in ultrasound images while preserving the structural details and quality better than the WGAN model. Furthermore, we can see from Table 5 that the best visual results correspond mainly to dataset A, whose original images had the lowest resolution compared to the other datasets.

To confirm the previous information, the test dataset (239 US images) was used to evaluate the data dispersion of the CGAN and WGAN algorithms using the PSNR and SSIM metrics.

Figure 4a–4d show the statistical results obtained using R software, where a and b show the dispersion data obtained by CGAN. The blue points represent the PSNR metric, which ranges from 30 to 40 dB, and the red points represent the SSIM metric, which ranges from 0 to 1.

Figure 4a and 4b show more signal of better image quality using CGAN network, it means better luminance (PSNR 36–42dB/SSIM 0.85 to 0.98), contrast and structural information in the restructured images by CGAN with respect to WGAN network (PSNR 36–48dB/SSIM 0.85 to 0.95) Fig. 4c and 4d.

5. Discussion

Ultrasound is a complementary technique to mammography and is used for breast cancer detection due to its sensitivity. However, the appearance of speckle noise in US is an interference mode that causes low

 ${\it Table 4} \\ {\it Visual comparison between original ultrasound RoI images and denoising images generated by Conditional GAN and WGAN}$

ID	Original	CGAN PSNR/SSIM	WGAN PSNR/SSIM
img_busi_34			
img_busi _70		40.18 dB / 0.9789	34.35 dB / 0.9535
img_busi _175		39.78 dB / 0.9717	35.77 dB / 0.9439
img_datasetA_6		39.40 dB / 0.9727	35.54 dB / 0.9423
img_datasetA_11		41.82 dB / 0.9776 42.15 dB / 0.9777	38.28 dB / 0.9655 38.29 dB / 0.9678

Table 4, continued

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ID	Original	CGAN PSNR/SSIM	WGAN PSNR/SSIM
img_datasetA_76			
		41.90 dB / 0.9776	38.42 dB / 0.9712
img_udiat_77	-6		
img_udiat_165		38.86 dB / 0.9676	36.41 dB / 0.9399
img_udiat_200		40.49 dB / 0.9672	33.38 dB / 0.9393
		37.97 dB / 0.9615	33.72 dB / 0.9185

contrast resolution [33], which makes it difficult to specialize in identifying abnormalities in the breast. In this paper, we trained a pair of GANs combined with CNN architectures as US image denoising, and then evaluated the quality of the denoised images using PSNR and SSIM metrics.

The quality of the denoising image in the Conditional GAN achieved a higher average PSNR (41.03 dB) and SSIM (0.97) in contrast to the average PSNR (35.47 dB) and SSIM (0.93) in the WGAN. Thus, according to the values given in Table 4, the CGAN is consistent with a higher quality image [63] and achieves success in ultrasound denoising images compared to the WGAN. This can be attributed to the fact that CGAN uses the Unet architecture as the generator model and Binary Cross Entropy (BCE) as the loss function (in addition to the L1 loss) [67,68] to generate real images and provide greater robustness to

Table 5
Comparison of the accuracy of our denoising method with others GAN and CNN denoising methods

Author	Method	Main idea	PSNR/SNR (dB)	SSIM	Acc/Sen/Spec (%)
Eckert et	MRDGet	DL method based on CNNs for mammogram	36.18	0.841	_
al. [11]		denoising to improve the image quality.			
Feng et	VGGNet	The network extracts the structure boundaries	30.57	0.90	_
al. [13]		before and after US image de-speckling			
Pang et al. [32]	TripleGAN	Method to perform data augmentation in breast US images.	_	_	90.41/ 87.94/85.86
		Then its images are used to classify breast masses using a CNN.			
Al-Dhabyani et al. [33]	AlexNet + GAN	US breast masses classification with data augmentation.			99/-/-
Vimala et al. [47]	Recurrent Neural Network	Hybrid deep learning technique to remove local speckle noise from breast US images.	70/65	_	_
Li et al. [72]	CGAN	WGAN loss are combined as the objective loss function to ensure the consistency of denoised image (lung and chest) and real image.	3326	0.92	
Huang, et al. [76]	DUGAN + UNET	Deep learning-based model for Low-dose CT denoising	34.6	0.91	_
Elhoseny and Shankar [77]	CNN	Edge preservation and effective noise removal in MRI and CT images. Then, CNN classifier is used to classify the denoised image as normal or abnormal	47.52	0.95	_
Ours	WGAN	Reduce speckle noise while preserving features	33.00	0.92	
	CGAN	and details in breast US images.	38.18	0.96	

the model. The Unet has an encoder-decoder network to reconstruct the despeckled image by extracting features from the noisy image to effectively enhance the image features and suppress some speckle noise during the encoding phase [69].

In contrast, WGAN uses Wasserstein distance and Resnet architecture as the generator model with gradient clipping as the loss function to achieve a 1-Lipschitz function. Although this network sometimes avoids the mode collapse problem, resulting in more stable training and less sensitivity to hyperparameter settings (because it is trained based on image distribution loss, rather than image pixel loss) [69], in this work the results generated by WGAN are not statistically significantly better than those generated by CGAN. For the previous reason Gulrajani et al. [70] proposed a WGAN with gradient penalty (GP) to replace the gradient clipping and to enforce Lipschitz continuity, which performs better and more stable training than WGAN with almost no hyperparameter setting

These performance differences in performance observed between the CGAN and the WGAN will also help to better implement new tasks in a computer system for detection/diagnosis of benign or malignant breast lesions. The pre-processing steps such as denoising, super resolution, or data augmentation based on deep learning algorithms help to improve the performance and accuracy in terms of clinical relevance in detection, diagnosis, segmentation, or image classification using CNN algorithms.

The main advantage of using GAN algorithms are the quality of the new images produced and the ability to generalize beyond the boundaries of the original dataset to produce new patterns.

Consequently, many researchers have been proposed a deep residual network structure based on GAN networks for image denoising.

Zhang et al. [71] used GANs Unet-based architecture as ultrasound image denoising, with residual dense connectivity and weighted joint loss (GAN-RW) to overcome the limitations of traditional denoising

algorithms. The results demonstrated that the noise level (PSNR = 3.08% and SSIM 1.84%) was effectively removed by the method, image detail was better preserved and the subjective visual effect was improved. Lan et al. [69] implemented a mixed-attention mechanism (MARU) with UNet model for real-time ultrasound image despeckle, using an encoder-decoder network to reconstruct the despeckled image by extracting features from the noisy image. Visual comparison shows that the proposed method outperforms the compared despeckling methods (SBF, SRAD, NML) in terms of speckle noise reduction and detail preservation.

The GAN-based combination methods have been applied to different tasks, and have achieved better results. For example [72], proposed a conditional GAN using a WGAN as an objective loss function in medical image denoising, the PSNR/SSIM values (29.4/0.88) demonstrated good results with respect to other state-of-the-art methods, perceiving the structure and details of the images.

Cantero J. [73] investigated two GANs (DCGAN and WGAN-GP) for the generation of synthetic PET (positron emission tomography) breast images. The visual results show that these two architectures can generate sinogram images that confound human evaluators. According to [74] the lower the amount of noise present in the real images the faster the DCGAN network learns to generate high fidelity images, but the results obtained here by WGAN-GP are not significantly better than those produced by DCGAN. In conclusion joint training of denoising and image classification significantly improves the performance of classification. A comparison of the accuracy of our work with more recent methods is shown in Table 5.

Finally, in this study, some limitations were presented, particularly in the availability of private data collection, because only public breast ultrasound databases were used. The implementation of hyperparameters in GAN training is very complex due to the sensitivity of their modification, generating some challenges (collapse mode, convergence, Nash equilibrium, and gradient), which are typical of generative networks. To minimize this problem during the training, it is essential to manually modify some hyperparameters (optimization functions, loss functions, number of epochs, layers, iterations), even to implement new alternatives based on deep convolutional networks to train the generator and the discriminator in a better way.

The research is reproducible, replicable and generalizable, and all code, data and materials have been deposited in the Mendeley repository [75], where the information can be accessed and used by others.

6. Conclusions

In conclusion, in this work CGAN proved to be a useful tool with a better-quality result for denoising breast ultrasound images than the WGAN model. This was obtained by comparing the mean statistical values (PSNR and SSIM) of the GAN models. The higher robustness demonstrated by CGAN is attributed to the fact that the generator uses U-Net encoder-decoder architecture with BCE loss function to remove the speckle noise in a better way than the Resnet architecture used in WGAN. The proposed CGAN technique is particularly useful for small data sets with low variance. These networks are widely used for image generation or data augmentation, but their application in US image denoising is still limited. In future work, other advanced deep learning methods for denoising such as convolutional neural networks and autoencoders will be used, and additional features will be considered in denoising breast images such as PET, thermal, CT, MRI to improve the performance of breast lesion classification algorithms.

Author contributions

Conceptualization Y.J.-G. and V.L.; methodology Y.J.-G.; formal analysis, Y.J.-G., M.J.R.-Á, and V.L.; investigation Y.J.-G and O.V; resources, D.C, Y.S, L.E, A.S, C.S; writing original draft preparation Y.J.-G,

O.V; writing manuscript and editing, Y.J.-G., M.J.R.-Á, and V.L.; visualization, Y.J.-G.; supervision, M.J.R.-Á and V.L.; project administration, M.J.R.-Á and V.L.; funding acquisition, M.J. All authors have read and agreed to the published version of the manuscript.

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Conflict of interest

The authors declare no conflict of interest.

Data availability statement

The data that support the findings of this study are openly available in the Mendeley repository (https://data.mendeley.com/drafts/g3cmj46xyx) [75].

Abbreviations

BUSI

DCSI	Breast Chrasoana mages Bataset
BCE	Binary cross entropy
CT	Computer Tomography
CGAN	Conditional GAN
CNN	Convolutional neural network
CNR	Contrast to-noise ratio
D	Discriminator
GAN	Generative adversarial network
G	Generator
JS	Jensen Shannon
KL	Kullback-Leibler
KID	Kernel inception distance
MRI	Magnetic Resonance Image
MSE	Mean Square Error
PET	Positron Emission Tomography
PSNR	Peak Signal-to-Noise Ratio
RMSE	Root-Mean-Square Error
SNR	Signal-to-Noise Ratio
SSIM	Structural Similarity Index
ReLu	Rectified Linear Unit
UDIAT	Diagnostic Centre of the Parc Tauli Corporation
US	Ultrasound
WGAN	Wasserstein GAN

Breast Ultrasound Images Dataset

Supplementary data

The supplementary files are available to download from http://dx.doi.org/10.3233/IDA-230631.

References

- [1] Y. Satoh et al., Deep learning for image classification in dedicated breast positron emission tomography (dbPET), *Ann Nucl Med* 36 (2022), 401–410.
- [2] E.K. Park et al., Machine learning approaches to radiogenomics of breast cancer using low-dose perfusion computed tomography: Predicting prognostic biomarkers and molecular subtypes, *Scientific Reports* 9(1) (2019), 17847.
- [3] Y. Ji et al., Independent validation of machine learning in diagnosing breast Cancer on magnetic resonance imaging within a single institution, *Cancer Imaging* 19 (2019), 1–11.
- [4] W.M. Salama and M.H. Aly, Deep learning in mammography images segmentation and classification: Automated CNN approach, *Alexandria Engineering Journal* 60(5) (2021), 4701–4709.
- [5] Y. Xu et al., Medical breast ultrasound image segmentation by machine learning, Ultrasonics 91 (2019), 1–9.
- [6] T.L. Szabo, Diagnostic ultrasound imaging: inside out, Academic press, 2004.
- [7] N.M. Tole, Basic physics of ultrasonographic imaging, World Health Organization, 2005.
- [8] S. Wang et al., Speckle noise removal in ultrasound images by first-and second-order total variation, *Numerical Algorithms* 78 (2018), 513–533.
- [9] S. Kaji and K. Satoshi, Overview of image-to-image translation by use of deep neural networks: denoising, super-resolution, modality conversion, and reconstruction in medical imaging, *Igaku Butsuri: Nihon Igaku Butsuri Gakkai Kikanshi = Japanese Journal of Medical Physics: an Official Journal of Japan Society of Medical Physics* 40(4) (2020), 139–139.
- [10] I. Njeh et al., Speckle noise reduction in breast ultrasound images: SMU (SRAD median unsharp) approach, *Eighth International Multi-Conference on Systems, Signals & Devices. IEEE*, 2011.
- [11] D. Eckert et al., Deep learning-based denoising of mammographic images using physics-driven data augmentation, *Bildverarbeitung für* die Medizin 2020: Algorithmen-Systeme-Anwendungen. Proceedings des Workshops vom 15. bis 17. März 2020 in Berlin, Springer Fachmedien Wiesbaden, 2020.
- [12] H. Chen et al., Low-dose CT with a residual encoder-decoder convolutional neural network, *IEEE Transactions on Medical Imaging* 36(12) (2017), 2524–2535.
- [13] X. Feng, H. Qinghua and L. Xuelong, Ultrasound image de-speckling by a hybrid deep network with transferred filtering and structural prior, *Neurocomputing* 414 (2020), 346–355.
- [14] A.E. Ilesanmi and T.O. Ilesanmi, Methods for image denoising using convolutional neural network: a review, *Complex & Intelligent Systems* 7(5) (2021), 2179–2198.
- [15] E. Kang et al., Cycle-consistent adversarial denoising network for multiphase coronary CT angiography, *Medical Physics* 46(2) (2019), 550–562.
- [16] P. Li et al., Multi-scale residual denoising GAN model for producing super-resolution CTA images, *Journal of Ambient Intelligence and Humanized Computing* (2022), 1–10.
- [17] Q. Yang et al., Low-dose CT image denoising using a generative adversarial network with Wasserstein distance and perceptual loss, *IEEE transactions on Medical Imaging* 37(6) (2018), 1348–1357.
- [18] A.S. Ahmed, W.H. El-Behaidy and A.A. Youssif, Medical image denoising system based on stacked convolutional autoencoder for enhancing 2-dimensional gel electrophoresis noise reduction, *Biomedical Signal Processing and Control* 69 (2021), 102842.
- [19] M. Daoud et al., Content-based image retrieval for breast ultrasound images using convolutional autoencoders: A feasibility study, 2019 3rd International Conference on Bio-engineering for Smart Technologies (BioSMART), IEEE, 2019.
- [20] S.K. Ghosh, B. Biswajit and A. Ghosh, A novel stacked sparse denoising autoencoder for mammography restoration to visual interpretation of breast lesion, *Evolutionary Intelligence* 14 (2021), 133–149.
- [21] Y. Jiménez et al., Preprocessing fast filters and mass segmentation for mammography images, *Applications of Digital Image Processing XLIV*, SPIE, 2021, pp. 352–362.
- [22] K.G. Lore, A. Adedotun and S. Soumik, LLNet: A deep autoencoder approach to natural low-light image enhancement, *Pattern Recognition* 61 (2017), 650–662.
- [23] X. Chen and S. Qianli, Medical image denoising based on dictionary learning, *Biomedical Research* (0970-938X) 28(20) (2017).
- [24] J. Huang and Y. Xiaoping, Fast reduction of speckle noise in real ultrasound images, *Signal Processing* 93(4) (2013), 684–694.
- [25] M.N. Kohan and B. Hamid, Denoising medical images using calculus of variations, *Journal of Medical Signals and Sensors* 1(3) (2011), 184.

- [26] I. Njeh et al., Speckle noise reduction in breast ultrasound images: SMU (SRAD median unsharp) approach, *Eighth International Multi-Conference on Systems, Signals & Devices*, IEEE, 2011, pp. 1–6.
- [27] R. Dass, Speckle noise reduction of ultrasound images using BFO cascaded with wiener filter and discrete wavelet transform in homomorphic region, *Procedia Computer Science* 132 (2018), 1543–1551.
- [28] A.S. Beevi and S. Ratheesha, Speckle Noise Removal Using Spatial and Transform Domain Filters in Ultrasound Images, 2021 7th International Conference on Advanced Computing and Communication Systems (ICACCS), IEEE, 2021, pp. 291–297.
- [29] S. Pradeep and P. Nirmaladevi, A review on speckle noise reduction techniques in ultrasound medical images based on spatial domain, transform domain and CNN methods, *IOP Conference Series: Materials Science and Engineering*, IOP Publishing, 2021, pp. 012116.
- [30] P. Li et al., TPNet: A Novel Mesh Analysis Method via Topology Preservation and Perception Enhancement, *Computer Aided Geometric Design* (2023), 102219.
- [31] H. Wu et al., Perceptual metric-guided human image generation, *Integrated Computer-Aided Engineering* 29(2) (2022), 141–151.
- [32] T. Pang et al., Semi-supervised GAN-based radiomics model for data augmentation in breast ultrasound mass classification, *Computer Methods and Programs in Biomedicine* 203 (2021), 106018.
- [33] W. Al-Dhabyani et al., Deep learning approaches for data augmentation and classification of breast masses using ultrasound images, *Int. J. Adv. Comput. Sci. Appl* 10(5) (2019), 1–11.
- [34] V. Jain and S. Seung, Natural image denoising with convolutional networks, Advances in Neural Information Processing Ssystems 21 (2008).
- [35] S.D. Wickramaratne and M.S. Mahmud, Conditional-GAN based data augmentation for deep learning task classifier improvement using fNIRS data, *Frontiers in Big Data* 4 (2021), 659146.
- [36] E. Wu et al., Conditional infilling GANs for data augmentation in mammogram classification, *Image Analysis for Moving Organ, Breast, and Thoracic Images: Third International Workshop, RAMBO 2018, Fourth International Workshop, BIA 2018, and First International Workshop, TIA 2018, Held in Conjunction with MICCAI 2018, Granada, Spain, September 16 and 20, 2018, Proceedings 3*, Springer International Publishing, 2018, pp. 98–106.
- [37] Z. Zhou et al., Image quality improvement of hand-held ultrasound devices with a two-stage generative adversarial network, *IEEE Transactions on Biomedical Engineering* 67(1) (2019), 298–311.
- [38] L. Bargsten and A. Schlaefer, SpeckleGAN: a generative adversarial network with an adaptive speckle layer to augment limited training data for ultrasound image processing, *International Journal of Computer Assisted Radiology and Surgery* 15 (2020), 1427–1436.
- [39] H.G. Khor et al., Ultrasound speckle reduction using wavelet-based generative adversarial network, *IEEE Journal of Biomedical and Health Informatics* 26(7) (2022), 3080–3091.
- [40] D. Mishra et al., Ultrasound image enhancement using structure oriented adversarial network, *IEEE Signal Processing Letters* 25(9) (2018), 1349–1353.
- [41] F. Carrara et al., Combining gans and autoencoders for efficient anomaly detection, 2020 25th International Conference on Pattern Recognition (ICPR). IEEE, 2021, pp. 3939–3946.
- [42] Y. Yao et al., Conditional Variational Autoencoder with Balanced Pre-training for Generative Adversarial Networks, 2022 IEEE 9th International Conference on Data Science and Advanced Analytics (DSAA), IEEE, 2022, pp. 1–10.
- [43] H.J. Kim and D. Lee, Image denoising with conditional generative adversarial networks (CGAN) in low dose chest images, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment 954 (2020), 161914.
- [44] X. Zou et al., WGAN-Based Image Denoising Algorithm, *Journal of Global Information Management (JGIM)* 30(9) (2022), 1–20.
- [45] V.K. Singh et al., Conditional generative adversarial and convolutional networks for X-ray breast mass segmentation and shape classification, *Medical Image Computing and Computer Assisted Intervention MICCAI 2018: 21st International Conference, Granada, Spain, September 16–20, 2018, Proceedings, Part II 11.* Springer International Publishing, 2018, pp. 833–840.
- [46] Y. Zhang, C. Hu and K. Wenchi, Medical image denoising, Biomedical Image Synthesis and Simulation, Academic Press, 2022, 255–278.
- [47] B.B Vimala et al., Image Noise Removal in Ultrasound Breast Images Based on Hybrid Deep Learning Technique, Sensors 23(3) (2023), 1167.
- [48] D. Khaledyan, et al., Enhancing breast ultrasound segmentation through fine-tuning and optimization techniques: Sharp attention UNet, *Plos One* 18(12) (2023), e0289195.
- [49] S. Zama et al., Clinical Utility of Breast Ultrasound Images Synthesized by a Generative Adversarial Network, *Medicina* 60(1) (2023), 14.
- [50] M. Li et al., Medical image analysis using deep learning algorithms, Frontiers in Public Health 11 (2023), 1273253.

- [51] A.E. Ilesanmi and T.O. Ilesanmi, Methods for image denoising using convolutional neural network: a review, Complex & Intelligent Systems 7(5) (2021), 2179–2198.
- [52] W. Al-Dhabyani et al., Dataset of breast ultrasound images, Data in Brief 28 (2020), 104863.
- [53] P.S. Rodrigues, Breast ultrasound image, Mendeley Data 110.17632. (2017).
- [54] M.H. Yap et al., Automated breast ultrasound lesions detection using convolutional neural networks, IEEE Journal of Biomedical and Health Informatics 22(4) (2017), 1218–1226.
- [55] I. Goodfellow et al., Generative adversarial networks, Communications of the ACM 63(11) (2020), 139–144.
- [56] M. Gong et al., Generative adversarial networks in medical image processing, *Current Pharmaceutical Design* 27(15) (2021), 1856–1868.
- [57] A. Abusitta, E. Aïmeur and O.A. Wahab, Generative adversarial networks for mitigating biases in machine learning systems, arXiv preprint arXiv:190509972. (2019).
- [58] G. Douzas and F. Bacao, Effective data generation for imbalanced learning using conditional generative adversarial networks, *Expert Systems with Applications* 91 (2018), 464–471.
- [59] Y. Yu et al., Unsupervised representation learning with deep convolutional neural network for remote sensing images, *Image and Graphics: 9th International Conference, ICIG 2017, Shanghai, China, September 13–15, 2017, Revised Selected Papers, Part II 9.* Springer International Publishing, 2017, pp. 97–108.
- [60] P. Isola et al., Image-to-image translation with conditional adversarial networks, Proceedings of the IEEE conference on computer vision and pattern recognition, 2017, pp. 1125–1134.
- [61] O. Ronneberger, P. Fischer and T. Brox, U-net: Convolutional networks for biomedical image segmentation, Medical Image Computing and Computer-Assisted Intervention–MICCAI 2015: 18th International Conference, Munich, Germany, October 5-9, 2015, Proceedings, Part III 18, Springer International Publishing, 2015, pp. 234–241.
- [62] M. Arjovsky, S. Chintala and L. Bottou, Wasserstein generative adversarial networks, International conference on machine learning, PMLR, 2017, pp. 214–223.
- [63] K. He et al., Deep residual learning for image recognition, Proceedings of the IEEE conference on computer vision and pattern recognition, 2016, pp. 770–778..
- [64] A. Obukhov and M. Krasnyanskiy, Quality assessment method for GAN based on modified metrics inception score and Fréchet inception distance, Software Engineering Perspectives in Intelligent Systems: Proceedings of 4th Computational Methods in Systems and Software 2020, Vol. 14, Springer International Publishing, 2020, pp. 102–114.
- [65] S. Rajkumar and G. Malathi, A comparative analysis on image quality assessment for real time satellite images, *Indian J. Sci. Technol* 9(34) (2016), 1–11.
- [66] S. Rajkumar and G. Malathi, A comparative analysis on image quality assessment for real time satellite images, *Indian J. Sci. Technol* 9(34) (2016), 1–11.
- [67] M.T. Martinez and O.N. Heiner, Conditional generative adversarial networks for solving heat transfer problems, No. SAND-2020-10569, Sandia National Lab, (SNL-NM), Albuquerque, NM (United States), 2020.
- [68] N. Mohammadi, M.M. Doyley and M. Cetin, Regularization by adversarial learning for ultrasound elasticity imaging, 2021 29th European Signal Processing Conference (EUSIPCO), IEEE, 2021, pp. 611–615.
- [69] Y. Lan and X. Zhang, Real-time ultrasound image despeckling using mixed-attention mechanism based residual UNet, *IEEE Access* 8 (2020), 195327–195340.
- [70] I. Gulrajani et al., Improved training of wasserstein gans, Advances in Neural Information Processing Systems 30 (2017).
- [71] L. Zhang and J. Zhang, Ultrasound image denoising using generative adversarial networks with residual dense connectivity and weighted joint loss, *PeerJ Computer Science* 8 (2022), e873.
- [72] Y. Li et al., A novel medical image denoising method based on conditional generative adversarial network, *Computational and Mathematical Methods in Medicine* 2021 (2021), 1–11.
- [73] L. Cantero, A GAN approach to synthetic PET imaging generation for breast cancer diagnosis, Master's thesis, Universitat Oberta de Catalunya, 2021.
- [74] Y. Lei, J. Zhang and H. Shan, Strided self-supervised low-dose CT denoising for lung nodule classification, *Phenomics* 1 (2021), 257–268.
- [75] Y. Jimenez et al., Ultrasound Breast images denoising using Generative Adversarial Networks (GANs), *Mendeley Data* V1, (2023).
- [76] Z. Huang et al., DU-GAN: Generative adversarial networks with dual-domain U-Net-based discriminators for low-dose CT denoising, *IEEE Transactions on Instrumentation and Measurement* 71 (2021), 1–12.
- [77] M. Elhoseny and K. Shankar, Optimal bilateral filter and convolutional neural network based denoising method of medical image measurements, *Measurement* 143 (2019), 125–135.