

Optimizing Electrostatic Similarity for Virtual Screening: A New Methodology

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Abstract. Ligand Based Virtual Screening methods are widely used in drug discovery as filters for subsequent in-vitro and in-vivo characterization. Since the databases processed are enormously large, this pre-selection process requires the use of fast and precise methodologies. In this work, the similarity between compounds is measured in terms of electrostatic potential. To do so, we propose a new and alternative methodology, called LBVS-Electrostatic. Accordingly to the obtained results, we are able to conclude that many of the compounds proposed with our novel approach could not be discovered with the classical one.

Key words: virtual screening, shape similarity, electrostatic similarity.

1. Introduction

The constant increase in the size of the databases used in Drug Discovery requires efficient techniques and methods that can be used to select the compounds most similarly to a query molecule and at the lowest possible cost. One of these techniques is Virtual Screening (VS). VS is an in-silico technique that allows large libraries with millions of compounds to be processed in order to find new compounds related to a pharmacological query based on one or more features (Hamza *et al.*, 2012; Boström *et al.*, 2013; Kumar and Zhang, 2016; Wang *et al.*, 2009). This represents a great advantage over experimental methods such as High-Throughput Screening (HTS) in terms of efficiency, budget, time and development cost (Kar and Roy, 2013). The resulting compounds from VS are subsequently acquired and empirically tested in the laboratory. In addition, VS techniques are often used as a pre-filter for HTS (López-Ramos *et al.*, 2009). All these advantages have increased the popularity of these techniques, which have experienced great advances over the last two decades. The interested reader is referred to previous works (Lešnik *et al.*, 2015; Kalászi

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et al., 2014; Liu *et al.*, 2011; Dou *et al.*, 2018; Schmidt *et al.*, 2018) for a description of different methods and tools currently used on VS.

However, there is still room for improvement regarding the accuracy of VS predictions so as not to discard promising compounds, or to reduce the time and error of calculations that compute the different features of the studied compounds (Böhm and Stahl, 2003). VS applied to the electrostatic similarity of compounds is a clear example of this. Contrary to what happens when VS is applied to select the most similar compounds in shape or pharmacophore properties, where the tools base their predictions on scoring functions that measure these particular features (Lešnik *et al.*, 2015; Puertas-Martín *et al.*, 2019; Yan *et al.*, 2013), the predictions in this field are not exclusively based on this descriptor, but on both the similarity of the three dimensional shape and electrostatic similarity (Tresadern *et al.*, 2009; Chu and Gochin, 2013; Kim *et al.*, 2015; Kossmann *et al.*, 2016; Woodring *et al.*, 2017; Maccari *et al.*, 2011; Kim *et al.*, 2016; López-Ramos and Perruccio, 2010; Hevener *et al.*, 2012; Kaoud *et al.*, 2012; Tiikkainen *et al.*, 2009; Massarotti *et al.*, 2014; Oyarzabal *et al.*, 2009).

Broadly speaking, all the previous works follow the same methodology, called LBVS-Shape throughout this paper, although they may differ in the selection procedure used to determine the compounds proposed as best predictions. Essentially, they initially optimize the compounds in the database against the query in terms of shape by using ROCS (OpenEye Scientific Software, 2019a). After that they select a number N of compounds with the highest shape similarity values and then finally evaluate them in terms of electrostatic similarity.

The value of N is not fixed, as it depends on the particular study. Usually, N is less than 10% of the total compounds in the database (Kossmann *et al.*, 2016; Hevener *et al.*, 2012; Kaoud *et al.*, 2012). A search for the best compounds basing on shape pre-filtering may be counterproductive, since the selection of a low value of N can rule many promising compounds out, which may have a significant impact on the final results.

Additionally, we also believe that using a more realistic description of compound bioactivity during the optimization procedure may help to obtain better predictions. As such, we propose a new approach as part of this work, named LBVS-Electrostatic, which involves the direct optimization of the electrostatic similarity. To do so, a new version of the algorithm OptiPharm, called OptiPharm_ES, has been implemented. OptiPharm (Puertas-Martín *et al.*, 2019) was initially designed to optimize the shape similarity between two given molecules, but now it has been adapted to maximize the electrostatic similarity. As results will show, the new LBVS-Electrostatic methodology is able to obtain better solutions than the ones obtained with the classical LBVS-Shape approach.

The rest of the paper is organized as follows. Section 2 gives a brief description about the mathematical formulation of the scoring functions. Sections 3 and 4 describe the two methods used for virtual screening based on electrostatic similarity, both the literature approach and the novel proposal. The former is currently the method most frequently used in the literature. In short, it computes a sublist of molecules with the highest three-dimensional shape similarity. Usually, such a sublist is only composed of less than 10% of

the total number of compounds in the database. From the reduced list, the compound(s) with the greatest electrostatic similarity is/are selected. The second one involves the resolution of an optimization problem guided by an electrostatic similarity function. Section 5 describes the framework where the experiments have been carried out and the main results obtained. Finally, the conclusions and lines for future research are summarized in the last section.

2. Scoring Functions to Measure Similarity Between Compounds

This section is devoted to defining the mathematical functions used to guide the searching processes. The figures in which the values of these objective functions are graphically represented have been created with VIDA v4.4.0 (OpenEye Scientific Software, 2019b) using the default configuration.

2.1. Shape Similarity

The shape similarity of two compounds is calculated as follows:

$$V_{AB}^g = \sum_{i \in A, j \in B} V_{ij}^g = \sum_{i \in A, j \in B} p_i p_j K_{ij} \left(\frac{\pi}{\alpha_i + \alpha_j} \right)^{\frac{3}{2}}, \quad (1)$$

where p_i and p_j are set to 2.7, α_i and α_j obtain the van der Waals value for each atom and

$$K_{ij} = \exp\left(-\frac{\alpha_i \alpha_j R_{ij}^2}{\alpha_i + \alpha_j}\right), \quad (2)$$

where R_{ij} is the distance between atoms i and j .

Notice that the accuracy obtained from (1) depends on the number of atoms in the two compared molecules, i.e. the higher this number, the longer the value of V_{AB} as an absolute value. To be able to measure the level of similarity between compounds, regardless of the number of atoms that they are composed of and the descriptor used, the Tanimoto Similarity (Jaccard, 1901) value is computed as follows:

$$Tc_s = \frac{V_{AB}}{V_{AA} + V_{BB} - V_{AB}}, \quad (3)$$

where V_{AB} is the A molecule overlaid onto B molecule. V_{AA} and V_{BB} is the overlap of the molecules A and B , respectively. (3) has a value in the range $[0, 1]$, where 0 means there is no overlapping and 1 means the shape of both molecules is the same.

2.2. Electrostatic Similarity

The electrostatic similarities are obtained by numerical solution of the Poisson equation (Böttcher *et al.*, 1974), viz:

$$\nabla\{\epsilon(r)\nabla\phi(r)\} = -\rho_{mol}(r), \quad (4)$$

where $\phi(r)$ is the electrostatic potential, $\epsilon(r)$ is the dielectric constant, and $\rho_{mol}(r)$ is the molecular charge distribution. Electrostatic similarity between two compounds is compared by determining E_{AB} :

$$E_{AB} = \int \phi^A(r)\phi^B(r)\Theta^A(r)\Theta^B(r)d\mathbf{r} \approx h^3 \sum_{ijk} \phi_{ijk}^A \phi_{ijk}^B \Theta_{ijk}^A \Theta_{ijk}^B, \quad (5)$$

where Θ is a masking function to ensure potentials interior to the compound are not considered part of the comparison. The integral appearing in (5) is a volume integral, computed using a grid-spacing parameter, h .

Again the accuracy obtained by (5) depends on the number of atoms in the compared molecules. As such, similarly to what was done previously, the Tanimoto Similarity (Jacard, 1901) value has been computed as follows:

$$T_{CE} = \frac{E_{AB}}{E_{AA} + E_{BB} - E_{AB}}, \quad (6)$$

where E_{AB} is the A molecule overlaid onto B molecule. E_{AA} and E_{BB} is the overlap of the molecules A and B , respectively. In this case, (6) has a value in the range $[-0.33, 1]$, where -0.33 means the charges of both compounds have the same value but opposite loads, 0 means there is no overlapping, and 1 means the charges of both molecules are the same.

3. The Previous Approach: The LBVS Method Guided by Molecular Shape (LBVS-Shape)

This method bases its predictions on a previous pre-filtering process consisting of identifying the N candidate compounds from the database with the highest shape similarity. After that, for each selected compound, the electrostatic similarity is calculated at the optimum superimposition obtained in the previous stage. Finally, the molecule with the highest electrostatic similarity value is selected as the one for the solution.

In this work, we have used the tool ROCS (OpenEye Scientific Software, 2019a) to optimize the shape similarity between two molecules. ROCS is a parametrized piece of software used to maximize volume overlapping similarity and utilizes the previously described (3) to represent molecules by means of Gaussian functions (Grant and Pickup, 1995; Grant *et al.*, 1996). Electrostatic similarity has been calculated using the ZAP Toolkit (see (6)).

This software has been downloaded without modification from the original website (OpenEye Scientific Software, 2019c). It is worth mentioning that ROCS and ZAP are, by far, the most widely used tools in the literature for VS based on shape and electrostatic similarity (Ellingson *et al.*, 2010; Thomas *et al.*, 2013; Hawkins and Stahl, 2018; Connelly *et al.*, 2015; Gowthaman *et al.*, 2015). For this reason they have been selected as part of this study; i.e. a fair and complete study must be carried out by making a comparison with the state-of-the-art methods.

4. The New Approach: A LBVS Method Guided by Electrostatic Similarity (LBVS-Electrostatic)

Our main aim when using this approach is to obtain the compound(s) with the highest electrostatic similarity values. Thus, an optimization problem must be defined with this aim in mind. Broadly speaking, any tool, method or algorithm used will be better guided towards the optima if the objective function is a numerical model representing the real objective. Until now, most methods focus on prioritizing the search of compounds with the same global shape, while they place electrostatic similarities at much lower priority. Consequently, they solve a shape similarity optimization problem instead of focusing on the electrostatic similarity, which may be more useful from the drug discovery point of view.

The new approach being presented here is based on the idea that the scoring function used to guide the optimization method must be mainly based on electrostatic similarity, since it is very likely that compounds with very high electrostatic similarity will share very similar chemical properties. The same can not be said while just focusing on shape similarity. In the latter, the search may converge to a sub-optimal solution (Ivorra *et al.*, 2018; Fernández *et al.*, 2017, 2019). OptiPharm (Puertas-Martín *et al.*, 2019), a recent algorithm proposed for working on LBVS problems, is used to prove our hypothesis. The interested reader is referred to as Puertas-Martín *et al.* (2019) for an in-depth description of this algorithm. For the sake of completeness, some of its main strengths and important features are briefly described in the following.

OptiPharm is a global evolutionary optimizer that can solve any optimization problem that concerns the computation of the similarity of two compounds, named query and target. It implements procedures to increasingly adjust the query molecule to the target, which remains fixed throughout the optimization method. A solution s represents the rotation and translation of the query with respect to the target. The parameters associated with s are dynamically bounded for each particular instance to reduce as much as possible the feasible region.

OptiPharm analyses the entire search space looking for likely areas where the local and global optima can be. To do so, it runs on a set of M solutions, called population, on which it applies a sequence of reproduction, selection and improvement procedures during several iterations.

Each solution in the population has a radius value that delimits a multidimensional subarea of the search space where the reproduction and improvement methods are applied.

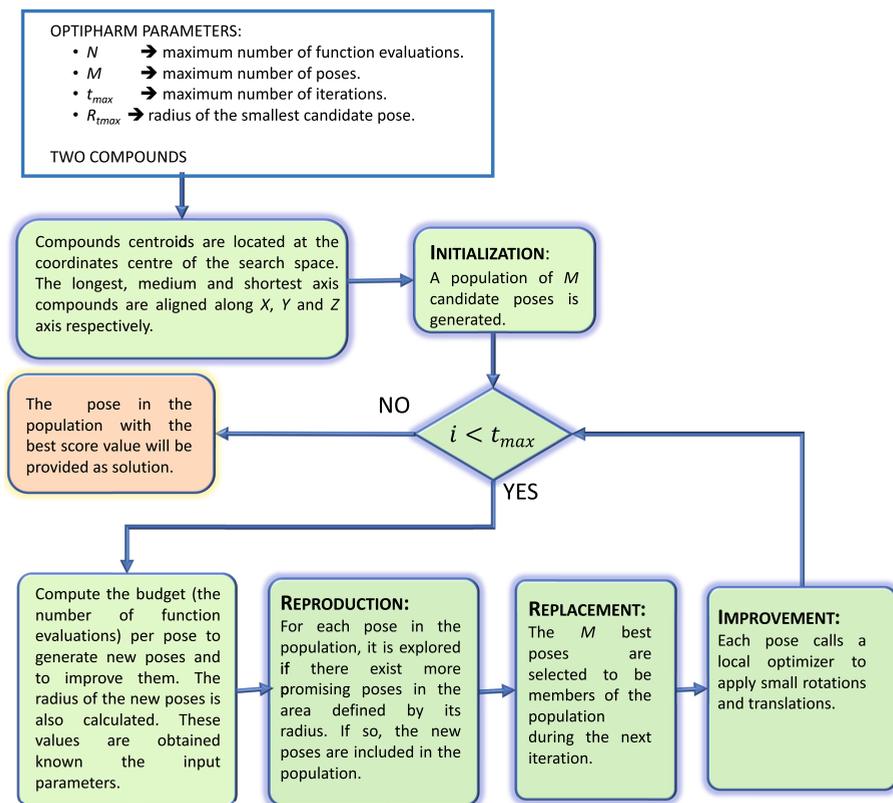


Fig. 1. OptiPharm algorithm: main stages.

The radius corresponding to a solution depends on the iteration i where it was created. The real strength of the radius is that it allows us to focus the search on different subareas since many solutions with different radii can coexist simultaneously during the optimization procedure. Therefore, at the same stage of the optimization procedure, new promising regions are systematically analysed, while others are examined thoroughly. Besides, the maximum number of initial solutions M , the number of iterations t_{max} and the smallest radius value $R_{t_{max}}$ OptiPharm has, as input parameter, a maximum number N of function evaluations.

Figure 1 shows the main stages of the algorithm and a brief description of the procedures implemented.

During this work, the scope of its functionalities has been extended to include the electrostatic potential as the scoring function. The new version has been called OptiPharm_ES. The electrostatic similarity between two compounds has been computed by using the source code of the ZAP Toolkit, also downloaded from <https://docs.eyesopen.com/toolkits/cpp/zaptk/thewayofzap.html> (OpenEye Scientific Software, 2019c). This approach ensures that the comparisons between methodologies are made under the same conditions. Additionally, OptiPharm_ES have been made available at <https://hpca.ual.es/optipharm/ES>.

4.1. Hardware Setup

All the experiments in this work have been executed using a Bullx R424-E3, which consists of 2 Intel Xeon E5 2650v2 (16 cores), 128 GB of RAM memory and 1 TB HDD (<http://hpca.ual.es/en/infraestructure>) along with the cluster Eagle <https://wiki.man.poznan.pl/hpc/index.php?title=Eagle>.

4.2. Benchmarks

In this work, a database provided by The Food and Drug Administration has been used (FDA). The Food and Drug Administration is a federal agency of the United States Department of Health and Human Services responsible for protecting and promoting public health by controlling, among other things, prescription and over-the-counter pharmaceutical drugs (medications). This agency provides a data set containing 1751 compounds, which represents approved medicines that can be safely used on humans in the USA. This database is useful since in the high similarity cases it would directly contribute to drug re-purposing. This is of relevant utility given the clear trend regarding re-purposing drugs observed over the last 5 years (Dakshanamurthy *et al.*, 2012; Kumar and Zhang, 2018; Yuan *et al.*, 2017).

The version of the database used in this work was obtained from DrugBank v5.0.1 (Wishart *et al.*, 2018) and necessary mol2 files for the VS calculations were set up by using AmberTools (Case *et al.*, 2017) by removing salts and neutralizing their protonation state, computing partial charges by MMFF94 force field, adding hydrogen atoms and minimizing energies (default parameters) (Halgren, 1995).

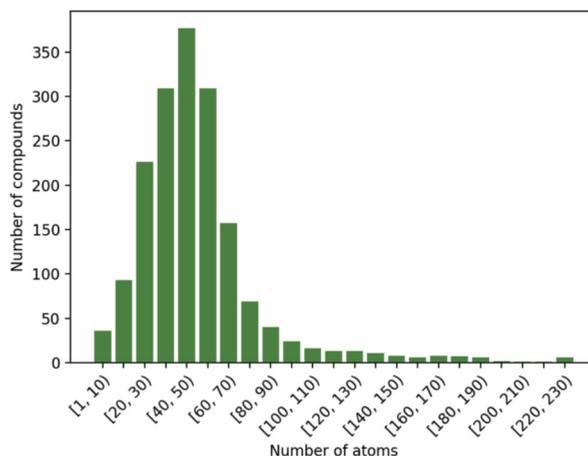
A comprehensive computational analysis may cover a representative sample of the database. The compounds included in the FDA database have different attributes, one of the most relevant for the study at hand being the number of atoms. In this work, a selection of 50 compounds has been made in the following way: the compounds in the database have been sorted by the number of atoms, including hydrogen, and then divided into 24 intervals (see Fig. 2). From each sector, at least one compound was chosen at random and proportional to the number of compounds in the sector.

Finally, these comparisons between compounds have been run using OptiPharm_ES with the following input parameter configuration: $N = 200000$ function evaluations, $M = 5$ starting poses, $t_{max} = 5$ iterations and $R_{t_{max}} = 1$ as the smallest possible radius.

5. Results

5.1. Influence of the Size List of Top-Ranked Compounds in the LBVS-Shape Method

As previously mentioned, the LBVS-Shape bases its predictions on a pre-selection of the first best compounds in terms of superimposition score (N). In this subsection, a study has been conducted to know how the value of N affects the final results from the point of view of electrostatic similarity. In particular, the LBVS-Shape has been performed on the



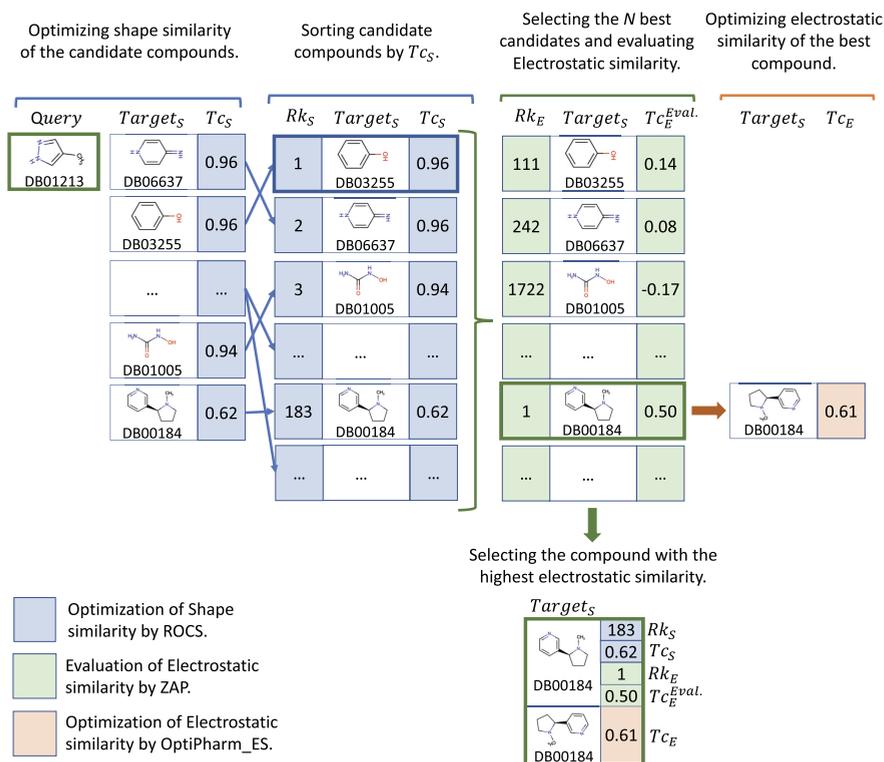


Fig. 3. Toy example of the performance of the LBVS-Shape method for a particular case where *Query* = DB01213 and *N* = 1751 using the FDA database.

Table 1

Influence of the parameter *N* in the results obtained by the LBVS-Shape method. For each value of *N*, the following average values from the 50 queries, are shown: position in the shape ranking ($Av(Rk_S)$), number of atoms ($Av(N_S)$), shape similarity score ($Av(Tc_S)$), electrostatic similarity evaluation score ($Av(Tc_E^{Eval})$) and electrostatic optimized similarity value (Tc_E).

<i>N</i>	$Av(Rk_S)$	$Av(N_S)$	$Av(Tc_S)$	$Av(Tc_E^{Eval})$	$Av(Tc_E)$
175	73	53	0.627	0.451	0.559
438	162	50	0.587	0.486	0.568
876	287	51	0.564	0.495	0.569
1313	324	50	0.559	0.497	0.570
1751	362	49	0.554	0.497	0.569

5.2. Performance Comparison Between LBVS-Shape and LBVS-Electrostatic Methods

To analyse the performance of both methods, we have conducted a study in which the selected 50 molecular queries are processed with reference to the FDA database. Notice that comparing a query with itself always reaches the maximum similarity value, both for electrostatic potential as well as for shape. Subsequently, these results were removed

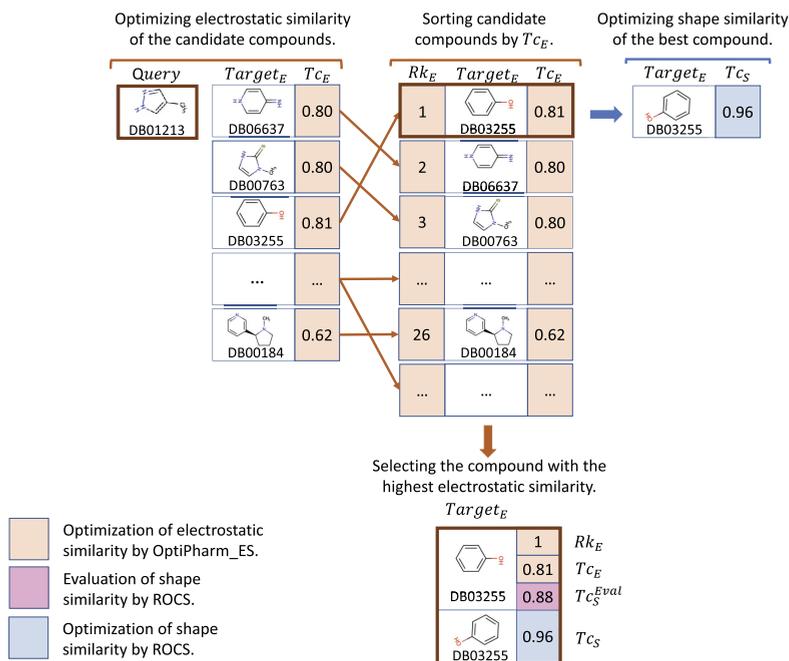


Fig. 4. An example of the performance of the LBVS-Electrostatic method for a particular case where *Query* = *DB01213* is compared to the FDA database.

when ranking the compounds. In other words, the compounds given as a result are not the most similar ones, but the second compounds in the ranked list. Additionally, as previously mentioned, the traditional method has been carried out considering the total number of compounds in the database $N = 1751$, so as to increase the probability of finding better predictions.

To illustrate how we generate the later summarizing tables, a sample of the results obtained by both methods when comparing a query to the molecules in the dataset is studied. In particular, the instance *Query* = *DB01213* is analysed. Notice that this is the example used to illustrate the stages of the LBVS-Shape method in Fig. 3. After that, the same instance is considered to exemplify the performance of the LBVS-Electrostatic method (see Fig. 4). Notice that this *Query* has been selected because it is small and it helps to see the main ideas of the paper very easily by using figures. However, the conclusions inferred from the associated results can be extrapolated to any other *Query*. As can be observed, the LBVS-Electrostatic technique solves an optimization problem to determine the electrostatic similarity, T_{c_E} , between the pharmaceutical *Query* and every *Target_E* in the database. Afterwards, the list of compounds is sorted by the T_{c_E} value and the one located in first position, $Rk_E = 1$, is selected as the best prediction. Finally, to complete the study, optimization is carried out to calculate the shape similarity T_{c_S} between the chosen compound and the *Query*.

For the sake of clarity and comparison, the results shown in Figs. 3 and 4 are summarized in Table 2. The meaning of the columns as well as the particular values in the tables,

Table 2

Summary of the results obtained for both LBVS-Shape and LBVS-Electrostatic methods for the query compound DB01213. The column notation, the colours included and the corresponding results come from Figs. 3 and 4, i.e. they maintain the same meaning as shown previously for those pictures. The last row indicates the results associated with the top solution selected for each method.

Query	N_Q	LBVS-Shape						LBVS-Electrostatic						
		Rk_S	$Target_S$	N_S	Tc_S	Rk_E^{Eval}	Tc_E^{Eval}	Tc_E	Rk_E	$Target_E$	N_E	Tc_E	Tc_S^{Eval}	Tc_S
DB01213	12	1	DB03255	13	0.963	111	0.140		1	DB03255	13	0.810	0.880	
		2	DB06637	13	0.961	242	0.081		2	DB06637	13	0.798	0.885	
		3	DB01005	9	0.943	1722	-0.172		3	DB00763	13	0.796	0.845	
	
		183	DB00184	26	0.621	1	0.500		110	DB00184	26	0.609	0.319	
		
DB01213	12	183	DB00184	26	0.621	1	0.500	0.609	1	DB03255	13	0.810	0.880	0.963

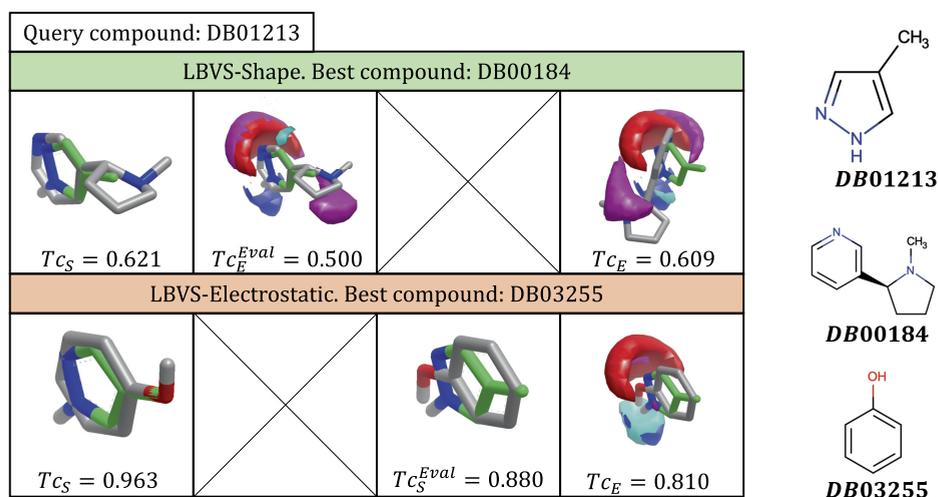


Fig. 5. Summary of results of LBVS-Shape and LBVS-Electrostatic where $Query = DB01213$. The Query compound is coloured green. Query electrostatic fields are coloured deep blue and red. Best compounds are shown in grey and their electrostatic potential fields, in light blue and pink.

are the ones previously explained and shown in each figure. The last row corresponds to the values associated with the best predictions. As can be observed, each method obtains a different compound as a top solution. LBVS-Shape provides the DB00184 molecule with a $Tc_S = 0.621$ and a $Tc_E^{Eval} = 0.500$. At the same time, LBVS-Electrostatic proposes the DB03255 compound as being the most similar to the query with $Tc_E = 0.810$ and $Tc_S^{Eval} = 0.880$. As such, the LBVS-Electrostatic method has not only obtained a more similar compound in terms of electrostatic potential, but also in shape. In Fig. 5, the final position for each case is shown.

Once the specific case of DB01213 has been explained in detail, the results of the 50 queries have been summarized in Table 3. Columns Rk_E^{Eval} and Rk_E have been removed in this table because their values are always 1. The last row summarizes the average of the results.

Table 3

Rows are sorted by the number of atoms of queries. For each query, the same procedure explained in Table 2 is followed. The last row summarizes the average values for each column.

Query	N_Q	LBVS-Shape						LBVS-Electrostatic				
		Rk_S	$Target_S$	N_S	Tc_S	Tc_E^{Eval}	Tc_E	$Target_E$	N_E	Tc_E	Tc_S^{Eval}	Tc_S
DB00529	10	316	DB05266	35	0.496	0.437	0.593	DB00818	31	0.720	0.468	0.614
DB01213	12	182	DB00184	26	0.621	0.500	0.609	DB03255	13	0.810	0.880	0.963
DB00173	15	102	DB00851	23	0.792	0.546	0.536	DB01119	21	0.834	0.777	0.830
DB00172	17	24	DB00128	16	0.881	0.469	0.561	DB00677	25	0.699	0.690	0.769
DB00331	20	380	DB00961	40	0.598	0.599	0.697	DB01018	24	0.790	0.559	0.649
DB01119	21	513	DB00828	15	0.655	0.519	0.613	DB00173	15	0.832	0.779	0.829
DB02513	25	27	DB01275	20	0.872	0.526	0.569	DB06637	13	0.915	0.745	0.805
DB00915	28	125	DB00160	13	0.684	0.404	0.543	DB00478	34	0.946	0.673	0.924
DB01352	29	1	DB00306	32	0.926	0.947	0.983	DB00306	32	0.983	0.901	0.926
DB01365	30	180	DB01191	33	0.738	0.902	0.960	DB01626	26	0.964	0.628	0.824
DB00657	33	47	DB06770	16	0.788	0.396	0.517	DB01043	34	0.979	0.609	0.861
DB00478	34	30	DB00752	21	0.787	0.508	0.637	DB01043	34	0.957	0.615	0.879
DB01043	34	27	DB00945	21	0.765	0.400	0.478	DB00657	33	0.973	0.711	0.861
DB00380	35	601	DB00731	50	0.620	0.380	0.407	DB08971	56	0.505	0.435	0.655
DB00693	37	1034	DB04575	59	0.525	0.362	0.429	DB00692	40	0.454	0.391	0.783
DB09185	37	243	DB01233	43	0.722	0.839	0.506	DB09021	39	0.916	0.429	0.650
DB07615	40	71	DB04552	28	0.704	0.861	0.866	DB09218	28	0.892	0.610	0.574
DB09219	40	123	DB00321	44	0.698	0.347	0.329	DB00316	20	0.450	0.249	0.462
DB00674	42	279	DB00575	23	0.688	0.505	0.653	DB00514	45	0.662	0.415	0.695
DB00887	45	209	DB00232	31	0.642	0.401	0.454	DB01127	39	0.662	0.378	0.576
DB01198	45	273	DB00209	59	0.648	0.748	0.768	DB00123	25	0.894	0.334	0.491
DB01155	48	1	DB01165	46	0.858	0.671	0.818	DB01208	50	0.899	0.385	0.835
DB00246	50	467	DB00268	44	0.542	0.843	0.852	DB05271	48	0.877	0.391	0.604
DB00381	53	525	DB00573	32	0.577	0.285	0.278	DB00630	27	0.377	0.397	0.524
DB00876	54	576	DB01002	49	0.516	0.395	0.505	DB00774	28	0.532	0.276	0.524
DB09237	54	380	DB09092	44	0.580	0.759	0.824	DB08998	40	0.902	0.447	0.596
DB00254	55	1100	DB00271	28	0.521	0.626	0.836	DB00271	28	0.836	0.219	0.521
DB01268	57	902	DB09014	54	0.518	0.792	0.765	DB01409	48	0.883	0.421	0.564
DB01196	60	7	DB00783	44	0.741	0.397	0.385	DB08797	17	0.527	0.195	0.385
DB01621	66	274	DB00268	44	0.552	0.821	0.845	DB04861	55	0.867	0.330	0.454
DB09236	66	459	DB00607	51	0.509	0.406	0.438	DB00449	54	0.664	0.439	0.551
DB00632	69	537	DB00511	123	0.348	0.067	0.246	DB00898	9	0.997	0.126	0.137
DB08903	69	6	DB01433	58	0.621	0.840	0.867	DB01359	51	0.888	0.307	0.464
DB01419	70	380	DB09209	61	0.431	0.854	0.879	DB01611	51	0.933	0.291	0.423
DB00320	80	204	DB00438	59	0.515	0.367	0.396	DB00120	23	0.563	0.245	0.278
DB00728	91	1383	DB06204	40	0.399	0.688	0.761	DB09131	3	0.874	0.068	0.101
DB00503	98	655	DB00206	84	0.371	0.256	0.243	DB01144	22	0.401	0.180	0.280
DB01232	100	639	DB06480	52	0.389	0.691	0.741	DB09089	58	0.791	0.290	0.387
DB00309	110	385	DB01603	45	0.455	0.241	0.297	DB00319	63	0.467	0.267	0.534
DB04786	120	4	DB09158	82	0.377	0.424	0.708	DB09159	18	0.910	0.108	0.120
DB09114	130	117	DB00595	57	0.376	0.273	0.506	DB00583	26	0.876	0.183	0.190
DB06439	137	657	DB01628	39	0.383	0.336	0.425	DB00878	64	0.488	0.274	0.423
DB01078	140	34	DB00204	56	0.424	0.201	0.259	DB01085	31	0.540	0.169	0.211
DB01590	151	1037	DB01193	53	0.265	0.248	0.358	DB00653	6	0.529	0.070	0.100
DB04894	152	82	DB01199	87	0.361	0.348	0.484	DB09131	3	0.662	0.006	0.040
DB00403	167	325	DB04855	84	0.261	0.325	0.395	DB06335	49	0.575	0.120	0.198
DB00732	169	640	DB08967	52	0.222	0.236	0.353	DB00653	6	0.508	0.051	0.069
DB00050	194	7	DB01369	141	0.349	0.238	0.383	DB00516	19	0.385	0.059	0.080
DB06699	221	1465	DB01245	56	0.119	0.365	0.513	DB09131	3	0.642	0.013	0.029
DB06219	229	69	DB01369	141	0.293	0.277	0.394	DB09131	3	0.670	0.009	0.021
Mean	74	362	–	49	0.554	0.497	0.569	–	31	0.738	0.372	0.505

As evidenced, LBVS-Electrostatic obtains on average $T_{c_E} = 0.738$, which is higher than that given by LBVS-Shape, $T_{c_E}^{Eval} = 0.497$. Similar conclusions can be inferred when comparing the T_{c_E} average values for both methods. Additionally, when the results are analysed individually, we can see that LBVS-Electrostatic provides solutions with higher T_{c_E} values than those achieved by LBVS-Shape. In fact, in 48 out of 50 cases, LBVS-Electrostatic obtains a different compound than that reached by LBVS-Shape.

Regarding shape similarity, it is possible to infer that, on average, the methods are equivalent in terms of accuracy of the predictions, i.e. LBVS-Shape obtains an average value of $T_{c_S} = 0.554$ while LBVS-Electrostatic reaches a mean value of $T_{c_S} = 0.505$. Furthermore, analysing the obtained results individually, we can see that in 2 out of 50 cases, LBVS-Electrostatic offers better or equivalent predictions than that achieved by LBVS-Shape in terms of shape (see columns T_{c_S} in LBVS-Shape and $T_{c_S}^{Eval}$ in LBVS-Electrostatic). It means that cases exist where two compounds can be very similar in terms of electrostatic potential, although they can be very different in terms of three-dimensional shape. It means that those solutions could not be obtained by using the methodology followed by the traditional LBVS-Shape method, since it only focuses on the compounds with the highest similarity in shape.

Making a somewhat more detailed approach for compounds smaller than 50 atoms, which means the first 23 query compounds in the table, there are 5 cases where the difference is less than 0.05 (DB00529, DB00173, DB00331, DB00915 and DB01352) and in another 3 cases the difference is 0.1 (DB01043, DB07615 and DB01268). Considering the values of these 7 cases in which the shape LBVS-Electrostatic is smaller than that of LBVS-Shape, the average difference is 0.048, while the mean gain in electrostatic similarity for those 7 compounds is 0.271. In large compounds, which includes 27 queries, there are only two cases with similar characteristics, which are compounds DB09236 with a difference of 0.07 and DB06699 with a difference of 0.013, both of them for shape similarity. In view of these results, the LBVS-Electrostatic method seems to be justified when proposing new solutions for small compounds.

However, not all the improvements are related to electrostatic fields. The optimization of electrostatic potential using OptiPharm_ES might allow a better solution to be found in terms of shape too. Compounds DB01119 and DB1213 in Table 3 are some outstanding examples. For example, in the case of *Query* = DB01119, the best compound found by LBVS-Shape is DB00828 with $T_{c_S} = 0.655$ and $T_{c_E}^{Eval} = 0.519$. Moreover, LBVS-Electrostatic's best compound is DB00173. It has a better T_{c_E} , i.e. 0.829, but also the position of those compounds after the electrostatic optimization is improved, $T_{c_S}^{Eval} = 0.779$.

5.3. ZAP Toolkit Accuracy Problem

The ZAP Toolkit has been widely used in the literature to calculate the electrostatic similarity score for two compounds (Boström *et al.*, 2013; Tresadern *et al.*, 2009; Chu and Gochin, 2013; Kim *et al.*, 2015; Kossmann *et al.*, 2016; Woodring *et al.*, 2017; Maccari *et al.*, 2011; Kim *et al.*, 2016; López-Ramos and Perruccio, 2010; Hevener *et al.*, 2012;

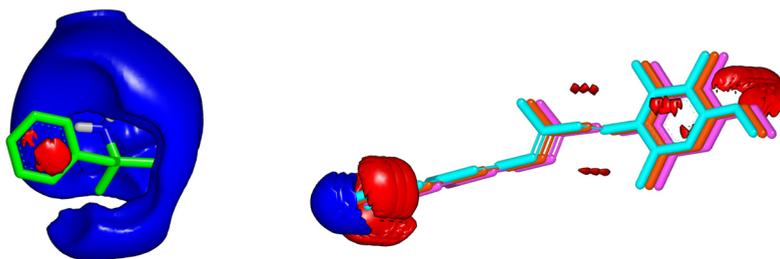


Fig. 6. Compound DB01365 is printed green. Compound DB00459 is represented in three coloured figures: light blue, red and pink. Electrostatic fields are printed in dark blue and red using VIDA.

Kaoud *et al.*, 2012; Tiikkainen *et al.*, 2009; Massarotti *et al.*, 2014; Oyarzabal *et al.*, 2009; Haque and Pande).

In this subsection we would like to remark that the ZAP Toolkit can return an erroneous value, which was discovered when using OptiPharm_ES. During the optimization procedure, OptiPharm_ES can progressively separate two input compounds aimed to escape from local optima and explore the searching space in depth. In fact, it is possible to analyse cases where no overlap exists between the input molecules. During the analysis of the results, we discovered that cases exist where the ZAP Toolkit can overflow, mainly when situations such as the previously mentioned happen. See Fig. 6 to see a particular example. Herein, compound DB01365 remains fixed on the left while compound DB00459 occupies three positions (red, blue and pink). The red compound obtains an electrostatic similarity value of 1. The light blue compound is displaced half a unit to the left, i.e. closer to the reference compound and its similarity value is 0.38. The pink compound is shifted 0.5 units to the right, that is, away from the reference compound. Its similarity value is 0. Calculations can be made using the ZAP Python script available at <https://docs.eyesopen.com/toolkits/python/zaptk/thewayofzap.html> in the Electrostatic Similarity section.

This problem has been solved in OptiPharm_ES by considering the poses with the previously mentioned problem unfeasible. It means that they are no longer considered during the optimization process.

6. Conclusions

In this work, a new approach to solve the LBVS problem based on the electrostatic similarity has been put forward. It has been called LBVS-Electrostatic. This methodology is based on the direct optimization of electrostatic similarity. For this purpose, a new version of OptiPharm has been used. Conversely, the method proposed in the literature, which has been named LBVS-Shape throughout the paper, looks for a sublist of the top compounds with the highest shape similarity by using ROCS, to later evaluate their electrostatic similarity with ZAP. In this work, a study to analyse the influence of the number of compounds in such a sublist has been carried out. As the results have shown, the larger the number

of molecules considered, the better the prediction obtained in terms of electrostatic similarity. From this conclusion, a computational study has been carried out to compare the new method LBVS-Electrostatic with the one in the literature LBVS-Shape. To increase the probability of finding good predictions, LBVS-Shape has been executed taking into account the whole database prior to the electrostatic similarity evaluation. Even so, LBVS-Electrostatic performs better than LBVS-Shape, achieving better predictions in electrostatic potential for the 50 queries included in the study. Regarding the shape similarity, both methods behave in a similar fashion, on average obtaining compounds with similar shape similarity values. It is important to mention that the new methodology proposed in this paper is novel, which means that the predictions proposed have not been analysed previously.

Finally, we have shown that ZAP can return erroneous values. This is an important discovery, since it is the most commonly used software in the literature to measure the electrostatic similarity.

In the future, we have plans to implement this objective function from scratch, but for the study at hand, we considered that it was more important to compare it with the state-of-the-art software. Additionally, other functions measuring the pharmacophore similarity will be implemented. Finally, we will analyse the problem from a multi-objective perspective, where shape and electrostatic similarity are optimized simultaneously.

A. Appendix Availability of data and materials

- Project name: OptiPharm_ES.
- Project home page: <https://hpca.ual.es/optipharm/ES/>.
- Project source code repository: https://gitlab.hpca.ual.es/savins/optipharm_es.
- Operating system(s): Linux and MacOS.
- Programming language: C++.
- License: Mozilla Public License 2.0.
- Any restrictions to use by non-academics: licence needed, contact with the authors.

The databases belong to their authors and access to them depends on any applicable restrictions.

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