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# A flood map based DOI decoding method for block detector: A GATE simulation study

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Abstract. Positron Emission Tomography (PET) systems using detectors with Depth of Interaction (DOI) capabilities could achieve higher spatial resolution and better image quality than those without DOI. Up till now, most DOI methods developed are not cost-efficient for a whole body PET system. In this paper, we present a DOI decoding method based on flood map for low-cost conventional block detector with four-PMT readout. Using this method, the DOI information can be directly extracted from the DOI-related crystal spot deformation in the flood map. GATE simulations are then carried out to validate the method, confirming a DOI sorting accuracy of 85.27%. Therefore, we conclude that this method has the potential to be applied in conventional detectors to achieve a reasonable DOI measurement without dramatically increasing their complexity and cost of an entire PET system.

Keywords: Positron emission tomography, depth of interaction, GATE simulation

## 1. Introduction

Positron Emission Tomography (PET), a widely applied imaging method in metabolism, neuroscience, and molecular imaging [1–3], generally uses detector modules consisting of discrete crystal array and photo detectors [4]. For crystals decoding, the flood map of the discrete crystal array is used to generate a LookUp Table. As traditional method only decodes the location of the discrete crystal, in some situations, DOI information existing in the flood map would be omitted when traditional method is employed. Traditional DOI method is adding complicated extra design for DOI in the detector, which would result in increased design complexity and reduced energy and time performance[1,5,6].

It has been proved that DOI information does exist in the flood map. In Yang's dual ended detector study, the flood map obtained by one end PSAPD experiences obvious changes while decoding spots get elongated in shape when the interaction depth increases [7]. Besides, some crystal mapping spots in the flood map have similar "ghosting" phenomenon as that in Wei's PMT Quadrant Sharing detector decoding study [8]. Up till now, for single crystal and single detector photoelectric sensor design, or single ended readout detector, no reports have been found to directly estimate gamma ray reaction depth using flood map.

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In nuclear medical imaging research, the Monte Carlo simulation software GATE (Geant4 Application for Tomographic Emission) is extensively used for simulations [9]. Because optical models of Geant4 have been added, GATE can now perform simulations for visible photons transmission, which helps to accurately predict the performance of PET detectors [10], especially in specular reflection models [11]. As a result, GATE acts as a suitable tool for DOI research.

In this paper, we propose a DOI identification method based on single-ended readout mapping decoding position, and GATE simulations are carried out to confirm the validity of this method.

# 2. Method

### 2.1. Detector module and decoding position analysis

As shown in Figure 1(a), traditional detector module is composed of a crystal array and 4 PMTs (Photo-Multiplier Tube). A light guide with several slots filled by reflective materials is coupled with the crystal array and the PMTs on two ends, respectively. In order to decode the interaction crystal, Anger Logic is used to generate the crystal decoding map called flood map, shown as Figure 1(b). In the flood map, each spot is corresponding to a discrete crystal element in the array. As for one spot, its decoding position of interaction in the same crystal varies due to interaction depth uncertainty, photon transmission randomness and signal acquisition error. As a result, for each crystal in the flood map, the decoding map gives a spot rather than a point.

Figure 2 analyzes the effects of different DOIs on decoding position in detail. Figure 2(a) gives one dimensional representation of the detector. As long as interaction occurs in the crystal (no matter at a, b or c), large amount of low-energy visible photons will be generated. Before being detected by the PMTs, these photons need to pass through the crystal and the light guide. During this process, the photons will get bounced back and forth by the ESR reflectors, resulting in different photon distributions on 4 PMT detection surfaces. Based on the distribution, one-dimensional decoding position can be calculated using Eq. (1). Figure 2(b) shows the simulated distribution when interactions occur at a and c depth.

$$position = PMT_{A} / (PMT_{A} + PMT_{B})$$
(1)

$$PMT_{A} = \int_{0}^{25} f(x) \, dx \tag{2}$$



Fig. 1. Traditional detector module and the decoding map.



(a) Photons detection of light sharing (b) Photon distributions of a and b interaction depths. based detector module in one dimension.

Fig. 2. Depth of interaction affects decoding position.

$$PMT_{B} = \int_{25}^{50} f(x) \, dx \tag{3}$$

where f(x) is the intensity distribution function of the photons. PMT<sub>A</sub> and PMT<sub>B</sub> are the energy intensity obtained by the two PMTs. Obviously, we have position<sub>a</sub> < position<sub>c</sub>, and the decoding position of b is between a and c. Therefore, the reason why the DOI information is included in the decoding position is theoretically explained.

# 2.2. DOI-encoding method

To summarize the DOI measurement method based on mapping decoding position, a flow chart is given in Figure 3. In order to establish the relation between DOI and decoding position, a large number of interactions (10,000 counts in the simulation) are simulated at different depths using Anger Logic method to determine the decoding position/coordinates. For each depth, a probability density function is obtained to describe the decoding position distribution. As a result, a series of two-dimensional probability density functions  $f_l(x,y)$  are generated. Afterwards, in the flood map, for each pixel (x,y) of the spot corresponding to the crystal, the expectation of interaction depth, d, can be calculated using

$$d = \frac{\sum [l \times f_l(x, y) \times \exp(-\mu l)]}{\sum [f_l(x, y) \times \exp(-\mu l)]}$$
(4)

where, exp (-ul) is used for attenuation correction. *l* and *u* are the interaction depth and the crystal linear attenuation coefficient respectively. For example, the linear attenuation coefficient of LYSO is 87 cm<sup>-1</sup> [12].



Fig. 3. Flow chart of DOI identification method based on mapping decoding position. Table 1

GATE simulation parameters	
Simulation parameter	Value
Scintillation material	LYSO
Crystal size	$4$ mm $\times$ $4$ mm $\times$ $25$ mm
Light yield	26,000 photons per MeV
Linear attenuation coefficient	0.87 cm-1 @ 511 keV
Visible light attenuation length	42 cm
Reflector material	ESR film VM2000
Reflector thickness	0.15 mm
Reflective coefficient	0.985
Light guide attenuation length	42 cm
PMT type	Hamamatsu R9800
PMT photon detection efficiency	25%

Therefore, the conversion map from decoding position to DOI can be obtained. Lastly, according to the DOI measurement requirements, the spot area is divided into several sub areas. As for unknown depth interactions, their DOIs can be estimated using their decoding position.

# 2.3. Simulation method

In this paper, we employ GATE for carrying out simulations with basic simulation parameters listed in Table 1. Besides, the reflection type is set to 100% "specular lobe distribution" and the surface type is set to "dielectric metal" to simulate the ESR film. The surface finish is set to "polished" with a deviation of reflective angle of 0.31° as measured by Janecek with a Dektak 150 surface profilometer on a mechanically polished surface [8]. 4 mm ×4 mm × 25mm LYSO crystal is selected as the scintillator, whose light yield is 26,000 photons per MeV. Absorbing length ( $\mu_{ab}$ =50 cm) and Rayleigh scattering length ( $\mu_{Rs}$ =260 cm) were constrained to a total attenuation length ( $\mu_{al}$ =42 cm) for LYSO [13]. The attenuation length in light guide is assumed the same. Linear attenuation coefficient of LYSO is 87 cm-1. The reflector is ESR film with the reflective coefficient of 0.985 [11]. The ratio of effective photons to light yield is 0.25, which included the light collection efficiency and photodetector quantum efficiency. The effective photons is calculated as  $26000 \times \frac{511}{1000} \times 25\% = 3321$  In order to short the computing time, the number of effective photons is directly used in simulation, and 3321 photons are used to represent the light output of Gamma ray with energy of 511 KeV. A Linux shell program is developed to call the GATE macro programs and Octave programs to generate and analyze the GATE simulation data, respectively.

# 2.4. Sorting accuracy

The Sorting Accuracy is used to assess the DOI method. For example, for a two-bin DOI method, the crystal is divided into two layers: the upper layer and the lower layer. For the depth belonging to the upper layer, a large number of events are simulated. The events sorted as the upper layer by the DOI method are true classification, and the events sorted as the lower layer are false classification. The sorting accuracy of the depth is the result of dividing the true classification by the total events. Total sorting accuracy of the DOI method is the average of the sorting accuracy of different depths.

# 3. Results and analysis

Figure 4 shows the conversion map from decoding position to DOI as calculated by weighting method.



Fig. 4. Conversion map between decoding position and DOI.



Fig. 5. Two layers of DOI segmentation for the crystal. (a) Spot region (conversion region). (b) Sub region corresponding to the interactions occur in the upper layer. (c) Sub region corresponding to interactions occur in the lower layer.



Fig. 6. Sorting accuracy as a function of depth.

For the most basic DOI measurement, namely dividing the crystal into two layers, a threshold equal to half of the crystal length is used to segment the conversion map and divide the spot region (Figure 5(a)) into two sub regions, as shown in Figures 5(b) and 5(c).

The segmentation region in Figure 5 is used to validate the accuracy of proposed DOI decoding method. In GATE simulations, the interaction depth varies from 2.5 to 22.5 mm, with a 1 mm gradient. Figure 6 summarizes the DOI sorting accuracy. As we can see, the sorting accuracy is high when the interactions occur at the two ends of the crystal, while it is low when interactions occur in the middle. Specifically, when the depth is 12.5 mm, due to the attenuation correction effect, DOI sorting accuracy is lower than 50%. However, attenuation correction improves the sorting accuracy when interactions occur in the upper half crystal, considering that the interaction taking to a exponential decay distribution along the crystal. According to the exponential distribution, weighted average of the 21 depths sorting accuracy is 85.27%.

### 4. Conclusion

In this paper, we propose a DOI decoding method based on flood map for low-cost conventional block detectors with four-PMT readout. Conversion map between decoding position and DOI needs to be established first, followed by dividing the spot area mapping one crystal in flood map into different sub regions, which correspond to different DOIs. As validated by the sorting accuracy of 85.27% in GATE based simulations, we conclude that this method can successfully realize the DOI measurement. In the future, we will assemble detectors and conduct relevant experiments to get some experimental evidence and try to apply the method into PET detector.

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