

Fuzzy optimization control for NO_x emissions from power plant boilers based on nonlinear optimization¹

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Abstract. Combustion optimization adjustment can effectively suppress NO_x emissions from power plant boilers. Current combustion optimization adjustment methods involve nonlinear optimization based on the boiler combustion model, such as optimization by a genetic algorithm or particle swarm algorithm. The computational complexity of these methods results in poor real-time performance, which limits their practical applications. To solve this problem, a fuzzy optimization control method with better real-time performance is proposed. First, the space of the disturbance variables (DV), which are the input variables that combustion systems cannot adjust, is divided into a certain number of sub-spaces. Each sub-space center is then obtained using the corresponding optimal combustion mode by offline nonlinear optimization, thereby forming a complete expert rule base. The corresponding optimal manipulated variables (MV), which are the input variables that combustion systems can adjust, are then quickly obtained online by means of fuzzy inference for each inputted DV. The fuzzy optimization control of boiler combustion adjustment is then determined. Simulation has shown that both the fuzzy optimization control method and the nonlinear optimization method can achieve a consistent control effect. However, the fuzzy optimization control method has a better real-time performance.

Keywords: NO_x emissions, combustion adjustment, nonlinear optimizing, fuzzy optimization control

1. Introduction

Combustion optimization adjustment can effectively suppress NO_x emissions from power plant boilers [23]. This adjustment ensures that the combustion condition adapts to the various operating conditions of the unit during boiler operation by adjusting the corresponding input parameters of the combustion system. Current combustion optimization adjustment methods involve nonlinear optimization based on the boiler combustion model, which often uses artificial neural networks,

support vector machines, and other modeling methods to establish a boiler combustion model. Nonlinear optimization is based on the theory of biological evolution; animal population movement is used to obtain optimal values for the combustion system output variables, which are then directly utilized to guide online dynamic adjustment. Wang, et al. [22] introduced the use of the neural network model to describe the boiler combustion process and the use of a genetic algorithm to determine the optimal oxygen content in fuel gas. Yin, et al. [10] proposed the use of support vector machines to establish both boiler thermal efficiencies and the NO_x emissions model. The group then optimized the model by PSO (Particle Swarm Optimization). However, the nonlinear optimization algorithm demonstrates poor real-time performance, is difficult to apply in engineering practice, and is time-consuming to improve.

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orthogonal experimental [7] and historical data sources [11, 12]. A selected portion of the modeling data is presented in Table 1.

The first 90 sets of data were selected as the training sample set, and the remaining 15 sets of data were selected as the test sample set. LS-SVM [8, 9] were used to establish NOx emission models. The modeling process is described in Equation 1.

$$\phi(NO_x) = f(DV, MV) \quad (1)$$

where $\phi(NO_x)$ represents the NOx emission, and f is the nonlinear model function of NOx emissions.

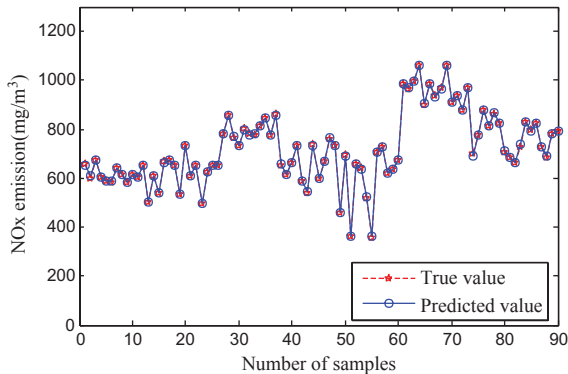


Fig. 2. Training sample error of LS-SVM model.

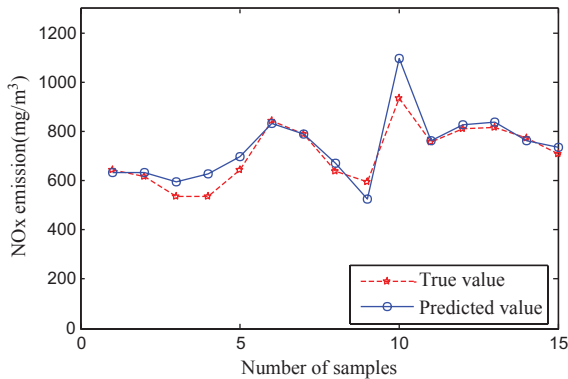


Fig. 3. Test sample error of LS-SVM model.

Table 2
LS-SVM model error

Training sampling error		Test sample error	
Absolute error (mg·m ⁻³)	Relative error (%)	Absolute Error (mg·m ⁻³)	Relative error (%)
1.5760	0.23	38.6923	5.73

Figure 2 shows the training sample error of the LS-SVM model, and Fig. 3 demonstrates the test sample error of the LS-SVM model. Absolute error was calculated according to Equation 2, relative error was calculated according to Equation 3, and the LS-SVM model error results are detailed in Table 2.

$$e_A = |y_P - y_T| \quad (2)$$

$$e_R = \frac{|y_P - y_T|}{y_T} \quad (3)$$

In Equations 2 and 3, e_A is the absolute error, e_R is the relative error, y_P is the predictive value, and y_T is the true value.

As shown in Table 2, the absolute error and the relative error of both training samples and test samples are exceptionally small. The output of the LS-SVM model is significantly close to the actual data, which indicates that the LS-SVM model is a useful approach in terms of performance, popularizing ability, and predictive accuracy.

3. Establishment of expert rule base based on the nonlinear optimization

3.1. Division of DV space

Three variables, L, Q, and V, were selected to constitute the DV space. First, the variables were normalized to fit in the same range [-1, 1]. The data was then converted to a dimensionless number. The ranges of standardized variables are denoted as domain U_L , U_Q , and U_V . According to engineering practice, five fuzzy subset centers were assigned, including -1, -0.5, 0, 0.5, and 1. The given fuzzy subset center belongs to the domain [-1, 1]. The isosceles triangle membership function curve was then selected (Fig. 4), and the U_L , U_Q , and U_V domains were simultaneously divided into five fuzzy subsets. The fuzzy word set was {VS, LS, MI, LB, VB} [2], where VS is Very Small, LS is Little Small, MI is Middle, LB is a Little Big, and VB is Very Big.

Domains U_L , U_Q , and U_V constitute a three-dimensional Euclidean space, which can also be referred to as an “ordered pair” (L, Q, V) [5]. The given fuzzy subset center combines freely as the form (L, Q, V). Each (L, Q, V) represents a set of combustion conditions. Since each fuzzy subset center represents a corresponding fuzzy subset, the 125 freely-combined

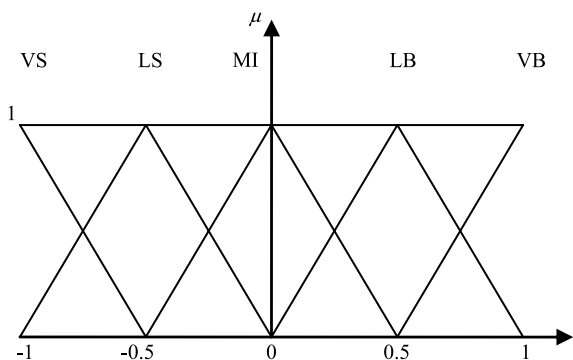


Fig. 4. Isosceles triangle membership function curve.

sets of combustion conditions can cover all actual combustion conditions. Each “ordered pair” (L, Q, V) also represents a corresponding subspace.

3.2. Establishment of expert rule base based on nonlinear optimization

Each subspace center corresponding to the optimal combustion mode based on the NOx emission LS-SVM model can be obtained by the nonlinear optimization [1, 3, 18], i.e., the MV optimal value corresponding to 125 sets of freely-combined fuzzy subset centers is obtained. To ensure the stability and safety of the unit operation, each MV must be adjusted to fall within a certain range. Therefore, each MV must be within the actual adjustment range in the optimizing process. The adjustment ranges of the MVs are shown in Table 4.

According to the MV adjustment ranges, 125 sets of fuzzy rules were obtained [13], which were used to constitute the expert rule base [16]. The form of fuzzy rules in the expert rule base can be expressed as:

$$\text{IF } DV, \text{ THEN } MV_{opt} \quad (4)$$

Table 3 Selected expert rule base data

DV			MV						
L (MW)	Q (%)	V (%)	P _A (KPa)	S _{EA} (%)	S _{EB} (%)	S _{EC} (%)	S _{RU} (%)	S _{RD} (%)	O ₂ (%)
238.78	22.79	9.02	3.83	37.76	1.02	67.81	64.65	20.05	3.00
238.87	22.65	8.95	3.70	48.26	2.34	68.50	63.95	20.41	3.03
...
302.47	22.31	9.94	3.46	92.50	1.67	69.96	53.90	21.24	3.01
302.48	20.93	9.60	3.09	91.97	1.32	64.99	50.52	79.66	3.18
...
291.08	23.34	9.00	2.94	93.51	1.18	69.97	46.84	79.96	3.53
291.48	23.74	8.80	4.04	30.73	1.16	69.69	62.37	20.96	3.02
...

A portion of the expert rule base data is shown in Table 3.

4. Fuzzy optimization control

4.1. The structure of optimization control system

After fuzzification and related fuzzy inference achieved by the fuzzy inference engine and expert rule base, the fuzzy linguistic variables are defuzzified to obtain the exact optimal MV value for each set of actual inputted DVs. The structure of the optimization control system is shown in Fig. 5.

4.2. Fuzzification for DV

Equation 5 is first used to standardize each input variable:

$$DV'_i = \frac{DV_i - \frac{DV_{i,max} + DV_{i,min}}{2}}{\frac{DV_{i,max} - DV_{i,min}}{2}} \quad (i = 1, 2, 3) \quad (5)$$

where DV'_i represents the standardized values of the three input DVs, including L, Q, and V; DV_i represents the three input DVs; $DV_{i,max}$ is the upper limit of the input DV; $DV_{i,min}$ is the lower limit of the input DV; and the three input DV values all belong to the domain [-1,1].

After standardization, each of the three input DV corresponding fuzzy subset membership degrees are obtained by the isosceles triangle membership func-

Table 4 Adjustment ranges of MVs

MV	P _A (KPa)	S _{EA} (%)	S _{EB} (%)	S _{EC} (%)	S _{RU} (%)	S _{RD} (%)	O ₂ (%)
Upper Limit	2.9	30	1	30	5	20	3
Lower Limit	4.2	94	38	70	65	80	4.5

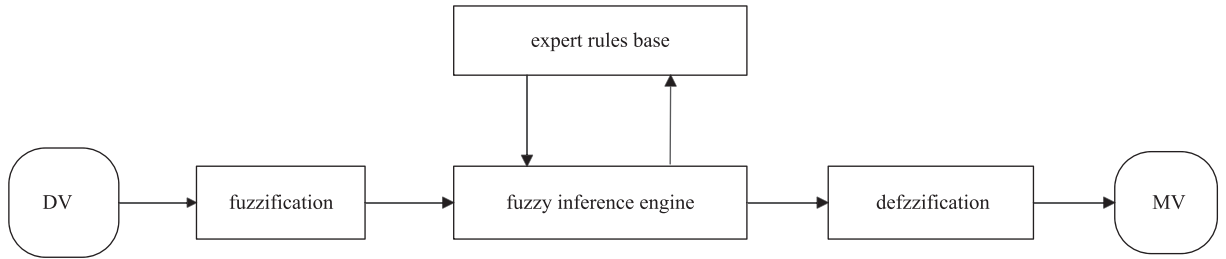


Fig. 5. Structure of the optimization control system.

tion (Fig. 5). The process of DV fuzzification is then complete.

4.3. Design of fuzzy inference engine

The fuzzy rules in the expert rule base are constituted by antecedent parameters [14] and consequent parameters. Antecedent parameters are freely combined fuzzy subset centers that are used to divide the DV space, and consequent parameters are corresponding optimal MV values obtained by nonlinear optimization, which can be expressed as $DV \Rightarrow MV_{opt}$. Additionally, the membership degree of every fuzzy subset center corresponding to fuzzy sets is 1. Equation 6 can be used to calculate the membership degree of each set of DV corresponding to fuzzy rules.

$$\mu_{DV} = \mu_{DV_L} \cdot \mu_{DV_Q} \cdot \mu_{DV_V} \quad (6)$$

After fuzzification of each DV inputted, there are two sets of fuzzy subsets that increase the corresponding membership degree to a positive value. Since the selected DV has three variables, there are eight types of fuzzy subset combinations, making each set of DV-corresponding fuzzy subset membership degree greater than zero. This can be described by corresponding fuzzy variables and level variables; each set of input DVs corresponds to eight sets of fuzzy rules in the expert rule base, which can be expressed as $DV_i \Rightarrow MV_{i_{opt}}$ ($i = 1, 2, \dots, 8$). Equation 6 is used to calculate the membership degree of each set of DVs corresponding to fuzzy rules. Each calculated value represents the membership degree of the DV input corresponding to fuzzy rules in the expert rule base.

4.4. Defuzzification

The fuzzy variables are converted to final exact values by a weighted average judgment method [6, 15], demonstrated by the following equation:

$$Y_{MV_{opt}} = \frac{\sum_{i=1}^8 \mu_i \cdot MV_i}{\sum_{i=1}^8 \mu_i} \quad (7)$$

where $Y_{MV_{opt}}$ is the final optimal MV; for each DV inputted, there are eight corresponding sets of fuzzy rules in the expert rule base. Thus, μ_i is the membership degree of the corresponding eight sets of fuzzy rules; MV_i represents the optimal MV; and the consequent parameters correspond to the eight sets of fuzzy rules.

5. Simulation study

The PC machine for simulation had the following characteristics: operating system, Windows 7; CPU, 2.5 GHz; and RAM, 4GB. A total of 105 sets of modeling data were selected, and the corresponding NOx emissions derived from the method based on nonlinear

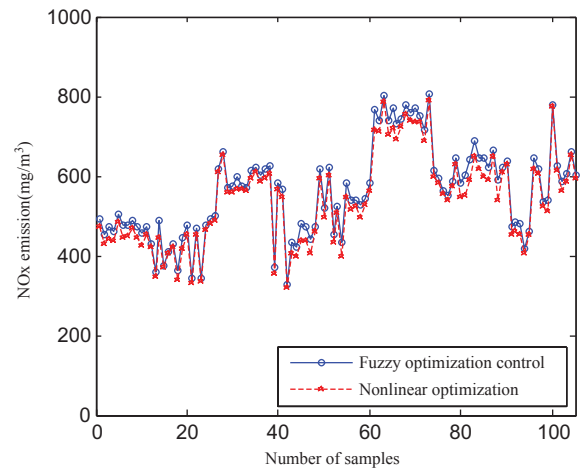


Fig. 6. Corresponding NOx emissions obtained by the fuzzy and nonlinear optimization methods.

optimization and the method based on fuzzy optimization control were compared (Fig. 6).

The predicted results based on fuzzy optimization control and the actual value are significantly close. The absolute error is 21.60896, and the relative error is 4.1396%. In addition to the similarity of results, they both meet environmental requirements. Moreover, the average time for each step of online optimization based on nonlinear optimization is 17.2s, while only 0.03s are required for each step of online optimization based on the fuzzy optimization control. It is evident that the online real-time optimization performance based on fuzzy optimization control is superior to the method based on nonlinear optimization.

6. Conclusions

Fuzzy optimization control based on the nonlinear optimization of power plant boiler NOx emissions can be described as follows: First, the DV space is divided into a certain number of subspaces. Each subspace center obtains an optimal corresponding combustion mode by offline nonlinear optimization, thereby forming a complete expert rule base. The corresponding optimal MV is then quickly obtained online by fuzzy interference for each inputted DV. The fuzzy optimization control for the boiler combustion adjustment is then realized.

Both the method based on nonlinear optimization and the method based on fuzzy optimization control can produce the same control effect. However, the optimization process based on the fuzzy optimization control method offers a simpler algorithm and fewer calculations, is less time-consuming online, and is more suitable for the real-time application of combustion adjustment.

The combustion model established by the orthogonal experiment can only reflect the current characteristics of the boiler; once the boiler equipment, coal or environmental factors change, the model can no longer accurately reflect the boiler situation. Thus, further research must be conducted to improve the adaptive capacity of the model.

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