Fuzzy logic-based multi-factor aided multiple-model filter for general aviation target tracking

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Abstract. A fuzzy logic-based multi-factor aided multiple-model filter (FLMAMMF) for General aviation (GA) maneuvering target tracking (MTT) is presented. The target category and meteorological information are introduced into the interacting multiple model (IMM) filter to perform GA target tracking. Fuzzy logic inference is employed in the proposed algorithm to reflect the complicated relationship between these two factors and the transition probability matrix (TPM). Both the number of models in model set and the transition probabilities between models are adjusted through fuzzy inference. Simulation results show that the proposed method is efficient and effective.

Keywords: General aviation target tracking, multi-factor Aided, IMM algorithm, model transition probability matrix, fuzzy inference

1. Introduction

For flight safety, an uninterrupted, reliable, accurate and effective monitoring of air traffic is crucial, especially for GA flights. Target tracking technology is the key to the GA aircraft monitoring system [12]. Over the years, many tracking methods have been developed, such as the differential polynomials, CV (constant velocity) and CA (constant acceleration) models, semi-Markov tracking filters, the "current" statistic models [9, 10]. These methods meet the tracking need of transport aviation ATC system but not that of GA, since there are a wide variety of GA aircrafts. GA aircrafts vary from ultra-light aircraft to small aircraft, powered to un-powered, manned to unmanned, etc. These wide variety of aircrafts have great difference in performance and flight mode. Furthermore, they flight at low altitude and are more influenced by meteorological environment. As a result, their flight trajectories show a strong maneuvering.

For maneuvering target tracking, Bar-Shalom and Blom proposed an algorithm called interactive multiple model (IMM) method, which is based on Generalized Pseudo-Bayesian algorithm (GPB) [3, 4]. The IMM uses a set of models to reflect different modes of maneuvering target and combines the output of multiple parallel filters (each with a different model) to get the global estimate. This filter has been successfully used in an ATC system [12]. However, flight model design is vital to the IMM algorithm and has a direct influence on the tracking result [1, 11]. This design should answer two basic questions: a) how many models are adequate to reflect such wide variety of GA targets, and b) how often does a flight change from one model to another. The first question can be easily solved when the type of GA aircraft is known. For example, an aircraft with ADS-B equipment can broadcasting its type along with its position to ATC system. The model set for each type
can be predefined. When the aircraft type is known, the corresponding model set can be employed by the IMM. When the type is unknown, one can identify the type by some target recognition methods or he has to use an over-fitted model set that will result in a bad global estimation.

The second one is the problem of how to setting transition probability matrix (TPM), which is obviously depend on the model set, i.e. the result of the first question. IMM algorithm commonly uses two methods to set the TPM when model set is determined, the off-line and the online methods. The off-line design method sets the TPM a priori as a design parameter. In the online method, the TPM is adaptable and is set by the process of quasi Bayesian estimator while filtering for tracking [6]. The existing TPM setting methods perform well when the affect of meteorological environment can be neglect, which is not the case in GA target tracking.

For better tracking of GA targets, the identified target type and the meteorological environment should be introduced into IMM. Since target recognition usually outputs the possibility of target types, the output is fuzzy in nature. Furthermore, meteorology (such as airflow) influence the flight in a complicated way, which can be modeled by fuzzy relations [2, 5, 7]. Considering of the above situations, a novel fuzzy logic-based multi-factor aided multiple-model filter (FLMAMMF) is proposed which employs the above influencing factors to adjust TPM. A set of fuzzy rules is designed according to the relationship of TPM with target category and meteorological environment. It gives a beneficial attempt to acquire better GA target tracking performance.

2. Problem formulation

In the IMM algorithm, the system of state equation and observation equation are given by

$$x_k = F_k(x_{k-1}, x_k) + w_k$$

$$z_k = H_k(x_k) + v_k$$

where $k$ is the time index, $x_k$ and $z_k$ represent the state and measurement vectors, respectively. $F_k$ and $H_k$ are the transition matrix and the observation matrix, respectively. The Gaussian white noise $w_k$ and $v_k$ are independent and their covariance are $Q_k$ and $R_k$, respectively. The parallel filtering system preset $r$ models work and $m_k$ is the model at time $k$.

IMM algorithm assumes the transition of the flight mode has homogeneous Markovian property. The probability of model $i$ at time $k$ transition to model $j$ at time $k+1$ is given by

$$p_{ij} = p(m_{k+1}^j | m_k^i) = \begin{bmatrix} p_{11} & \cdots & p_{1j} & \cdots & p_{1r} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ p_{ij} & \cdots & p_{ij} & \cdots & p_{ij} \\ \vdots & \ddots & \vdots & \ddots & \vdots \\ p_{ir} & \cdots & p_{ir} & \cdots & p_{rr} \end{bmatrix}$$

where $m_k^j$ is the filter model using at $k$ time, $m_{k+1}^j$ is that at time $k+1$.

The diagonal elements of the TPM between the model depend on the sojourn time in each motion model. The transition probability $p_{ii}$ depends on the expected sojourn time $\tau_i$ is given by

$$\tau_i = T \frac{1}{P_{ii}}$$

where $\tau_i$ is the expected sojourn time of the $i$th model, $P_{ii}$ is the probability of transition from $i$th model to the same model, and $T$ is the sampling interval. $P_{ii}$ are calculated using

$$P_{ii} = \min[hi, \max(l_i, 1 - \frac{T}{\tau_i})]$$

where $l_i = 0.1$ and $h_i = 0.95$ are the lower and upper limits, respectively, for the $i$th model transition probability. The selection of the off-diagonal elements of the TPM depends on the switching characteristics [8].

3. Selection of TPM

GA targets are diverse in category, and their performance differs greatly and is vulnerable to be influenced by meteorological environment. To achieve better GA target tracking this paper introduces the target category and meteorological information to adjust TPM.

3.1. Multi-factor aided adjust TPM

TPM in the IMM algorithm is given by

$$p_{ij} = P(m_{k+1}^j | m_k^i) = \frac{P(m_{k+1}^j,m_k^i)}{P(m_k^i)}$$

where

$$P(m_{k+1}^j,m_k^i) = \prod_{m=1}^r \{ p_{ij}^m \}$$
When influence factor $F_n$ is considered, it becomes

$$P_{ij} = \sum_n P(m_{i+1}^j | F_n, m_n^i)$$  (7)

According to Bayesian law,

$$P(m_{i+1}^j | F_n, m_n^i) = \frac{P(m_{i+1}^j | m_n^i) P(m_n^i | F_n)}{P(m_n^i)}$$

$$\cdots = P(m_{i+1}^j | m_n^i) P(m_n^i | F_n) P(F_n)$$

$$\cdots = P(m_{i+1}^j | m_n^i, F_n) P(F_n)$$  (8)

Target motion model has no relevance to $F_n$, so $P(F_n| m_n^i) = P(F_n)$, the TPM $P_{ij}$ is thus given by

$$P_{ij} = \sum_n P(m_{i+1}^j | m_n^i, F_n) P(F_n)$$  (9)

The influence factor mainly has two types: one for target category $c_i$ and one for meteorology $g_i$. The introduction of the target category information will first reduce the number of corresponding models and then be utilized to adjust TPM. It will improve the filtering accuracy and increase the speed of filter computation.

In GA target tracking, if the category of target exhibits weak maneuvering ability, the probability of staying in "current motion state" is small while that of transition to "other motion state" is large. If the category of target has strong maneuvering ability, the probability of staying in "current motion state" is small, and the transition probability to "other motion state" is large. But one thing remains the same, the sum of probability of staying in "current motion state" is always 1.

When airspace meteorological information $g_i$ changes, TPM needs to change accordingly. If a target is in good meteorological environment, then the maneuvering frequency will be relatively low, which suggests large diagonal elements of TPM and small off-diagonal elements. If a target is in bad meteorological environment, then its maneuvering frequency will be relatively high, thus the diagonal elements of TPM should be smaller and the off-diagonal elements be larger.

Considering these facts, target category and meteorological environment information can be used to determine TPM. Following the above relationship, the proposed algorithm adopt the fuzzy system to adjust the TPM for GA tracking.

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sets, ZE, SP, MP, VP, large positive (LP), and extremely large positive (EP), expressed as $\tilde{C}_s = 1, 2, \ldots, 6$. As shown in Fig. 3.

The membership function in each fuzzy set is determined in the following:

$$
\mu_{\tilde{A}_l i} (\Delta_{1c}^i) = 1 - \frac{|\Delta_{1c}^i - d_l^i|}{b_i} 
$$

where $\Delta_{1c}^i \in [d_l^i - b_l^i, d_l^i + b_l^i]$. Use the fuzzy IF-THEN rules to establish the fuzzy model of the relationship of $\Delta_{1\tau}^i$ with $\Delta_{1c}^i$ and $\Delta_{1g}^i$:

$$
R^i : \text{IF } \Delta_{1c}^i \in \tilde{A}_l \text{ AND } \Delta_{1g}^i \in \tilde{B}_j

\text{THEN } \Delta_{1\tau}^i \in \tilde{C}_s
$$

where $l = 1, 2, \ldots, M$, and $M = 16$. The designed fuzzy rule base is shown in Table 1.

As a result, the fuzzy system output is given as follows:

$$
\Delta_{1\tau}^i = \frac{\sum_{l=1}^{M} \left[ \min \left( \mu_{\tilde{A}_l i} (\Delta_{1c}^i), \mu_{\tilde{B}_j} (\Delta_{1g}^i) \right) \right]}{\sum_{l=1}^{M} \left[ \min \left( \mu_{\tilde{A}_l i} (\Delta_{1c}^i), \mu_{\tilde{B}_j} (\Delta_{1g}^i) \right) \right]} 
$$

(12)

$\Delta_{1\tau}^i$ can be applied to estimate TPM by using Equation (5).

4. FLMAMMF for hybrid estimation

FLMAMMF based on the original IMM algorithm adds the influence factors. A recursive cycle diagram of the algorithm is as shown in Fig. 4.

In this process, first using the current influence factor information (target category, meteorological environment information) to adaptively adjust TPM elements $P_{ij}$ to $P_{ij}^\prime$. The next step is interactive filtering, which is the same as in traditional IMM. Calculation of all the quantities is shown in Table 2.

5. Experimental results and analysis

5.1. Simulation setup

The simulational experiment is conducted by using a computer with a dual-core CPU of Pentium D 2.93 GHz, 2GB RAM. The programs are performed by using the Matlab 201 version software. The simulation results are derived from 100 Monte Carlo runs.

The first part: Simulated target motion trajectory is shown in Fig. 5. The simulation assumed that the target flight models be CV linear motion model and coordinated...
The simulation target is divided into seven phases: CT motion with turn rate $+\frac{3}{10}\degree/s$ between 15–30 seconds, CT motion with turn rate $-\frac{3}{10}\degree/s$ between 35–50 seconds, CT motion with turn rate $+\frac{5}{10}\degree/s$ between 55–70 seconds, CT motion with turn rate $-\frac{5}{10}\degree/s$ between 75–90 seconds, and constant velocity motion at the rest time. Simulation assumed that the target type information be unknown in the first 50 seconds. Filter initial model set is selected as follows: model 1: CV; model 2: CA; model 3: CT with turn rate $+\frac{3}{10}\degree/s$; model 4: CT with turn rate $-\frac{3}{10}\degree/s$; model 5: CT with turn rate $+\frac{5}{10}\degree/s$; model 6: CT with turn rate $-\frac{5}{10}\degree/s$; model 7: CT with turn rate $+\frac{7}{10}\degree/s$; model 8: CT with turn rate $-\frac{7}{10}\degree/s$; model 9: CT with turn rate $+\frac{10}{3}\degree/s$; model 10: CT with turn rate $-\frac{10}{3}\degree/s$. The initialization of TPM is selected as the $10 \times 10$ matrix:

$$
\begin{align*}
\mathbf{P}_0 &= \begin{bmatrix}
0.82 & \cdots & 0.02 \\
\vdots & \ddots & \vdots \\
0.02 & \cdots & 0.82
\end{bmatrix}
\end{align*}
$$

Fig. 5. The target trajectory 1.
After 50 seconds, target type information $F_1$ came, the fuzzy system adjusted the TPM to a $5 \times 5$ matrix and the model sets to the following: model 1: CV; model 2: CT with turn rate $+3^\circ/s$; model 3: CT with turn rate $-3^\circ/s$; model 4: CT with turn rate $+5^\circ/s$; model 5: CT with turn rate $-5^\circ/s$. The original models that do not conform to the target were abandoned.

The filtering results target motion trajectory 2 are shown in Fig. 9. It can be seen that FLMAMMF shows a superior performance to the fixed structure IMM algorithm, especially at the beginning of each maneuver, where the position and velocity RMSEs of the proposed algorithm is significantly reduced compared to the IMM algorithm.
6. Conclusion

The wide diverse categories of GA aircrafts are easily affected by meteorological environment in flight, which leads to the difficult problem of effectively track. This paper proposed a FLMAMMF for maneuvering GA target tracking. The relationship of target category and meteorological environment with the TPM is mapped into a set of fuzzy rules. By applying fuzzy logic in the standard IMM and designing the fuzzy system, the proposed algorithm introduces the target classification information and the meteorological environment information into the auxiliary filtering. Adjusting the model TPM by these two factors makes it more close to the actual flight mode, thus improves the tracking precision of the GA target, and reduce the computation time. Simulation experiments show that the estimation performance of the algorithm is better than that of the IMM algorithm. Future works may include introducing more influence factors and to quantify the influencing factors in further studies on the TPM.

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References